PERSON IDENTIFICATION BY FINGERPRINTS AND VOICE
The work was performed in 2005 – 2010 at Vilnius University

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Abstract

The purpose of this study is to investigate problematic areas that arise in biometrics and solve them. Two biometric technologies (fingerprint biometrics and voice biometrics) are addressed.

Fast synthetic fingerprint image generation is introduced. An application of using synthetic images with predefined properties to evaluate fingerprint extraction algorithm is proposed. An optimization technique that speeds up fingerprint image generation is described in detail. Correlation between synthetic and real fingerprints is evaluated.

Fingerprint matching algorithm that does not perform global registration and can match deformed fingerprints is described and evaluated.

New speaker identification method is presented and multibiometrics using fingerprints and voice is analyzed.

1 Introduction

1.1 Research Area

Biometric technologies are becoming very common in everyday life [1]. The use of distinctive and unique features that can identify a person (such as fingerprints, palm prints [2][3], face [31]), iris or voice) makes it possible to determine an identity of a person in easy and convenient way. Many countries integrate biometric features into the passports and identity cards. Biometrics is used at companies to track working time, identity is checked during elections to prevent multiple voting, at banks and in prisons to enforce security.

The use of biometric technology grows every day and is forecasted to grow in coming years what makes biometrics a very attractive branch of science. The research area of this work is fingerprint and voice biometrics: fingerprint
image synthesis for fingerprint extraction algorithm performance evaluation, distortion tolerant fingerprint matching, and speaker recognition.

1.2 Fingerprint biometrics
Fingerprint recognition is used for more than a hundred years. It is the most used biometric today. The usage of fingerprints for person identification became popular in Europe after Henry Fauld noticed in 1880 that fingerprints are unique and can be used to identify a person. In 1888 Francis Galton described features that can be used to identify fingerprints. In 1900 Edward Henry proposed fingerprint classification into six classes. This classification system is known as Henry system. Fingerprints are used by law enforcement agencies from the beginning of the XX century.

When fingerprints databases became large, manual identification became a difficult and problematic task. Starting from 1960 USA, Great Britain and France police departments and criminal investigation bureau were developing automatic fingerprint identification systems (AFIS). Nowadays AFIS is commonly used in law enforcement agencies around the world. Automatic fingerprint identification systems are also used in everyday life to enforce security in banks and in schools, to control access to computer accounts, and to track working time.

Although automatic fingerprint identification is used for more than fifty years, this task is not completely solved so attention to this branch of science is still high.

1.2.1 Fingerprint structure
Fingerprint is a structure of a fingertip lines (ridges and valleys) they appear during the early development of body and does not change much through the whole life. Burns, scratches and other imperfection can make a fingerprint less readable, but in most cases it is still possible to identify a person.
1.2.2 Fingerprint acquisition

Historically fingerprints were collected using ink and paper. A fingerprint was soaked in ink and pressed against a paper to get a plain fingerprint, or rolled on a paper from one side to another to get rolled fingerprint. Then a paper was scanned to get a digital image of a fingerprint. Fingertip has a sweat pores that constantly emit sweat and when a finger contacts other objects, thin film of sweat and fat is left on the surface of the object and represent a fingerprint that has left it. Such marks are collected by criminal investigators and used as an evidence of the crime scene. Such prints are called latent. Special chemicals are used to make them more evident, and digital photographs made. Latent fingerprints are often of poor quality and additional image processing is often performed before feature extraction. Most of the current civil and forensic biometric systems use fingerprint readers to obtain a fingerprint. Over the last decade, several companies released fingerprint scanners that provide good image quality, ease of use and attractive price. Almost all of the current fingerprint readers can be divided into three categories: optical (measuring light reflection on the finger lines and the spaces between them), semiconductor (directly measuring the characteristics
of a finger) and ultrasound (measuring the duration of the echo signal). Although optical scanners are the oldest and most commonly used, semiconductor scanners are becoming increasingly popular because they are lightweight and small, can be installed in portable computers, mobile phones and other devices. Semiconductor readers by the principle of operation are divided into capacitive, thermal and piezoelectric. Ultrasound scanners are not yet widely used because of bigger size and larger price. Most fingerprint scanners provide a flat image, but there are scanners that provide rolled fingerprint image. Scanners for rolled fingerprints are used for large scale AFIS and they are much more expensive than plain fingerprint scanners. The most important fingerprint scanner specifications are resolution, scanning area and the number of colors. Minimal resolution in accordance with the requirements of the FBI is 500 pixels per inch. If the resolution is lower, it becomes difficult to extract small features of a fingerprint. Readers with less than 250 pixels per inch resolution are not used in practice. According to the FB requirements, the area of the scanned fingerprint must be larger than $1 \times 1$ inches. Fingerprint color is not used in fingerprint recognition, so most fingerprint readers return gray-scale images.

### 1.2.3 Fingerprint features

Fingerprint image consists of lines (ridges and valleys) that go almost in parallel (Figure 1) Ridges sometimes split (bifurcate) into two or more ridges. Global patterns can be noticed in places where ridges are curved and change direction. Such areas of discontinuity are called singular points (Figure 2). There are three types of singular points [20]: core (*ridge lines make a 180 degree turnaround core point*), delta (ridges from three directions and connect in one point called delta) and whorl (ridge lines make a 360 degree turn around whorl point).
Figure 2: Singular points.

Figure 3: Minutiae points.
Local patterns can be noticed in places where ridge line bifurcates (splits into two ridges) terminates or connects. Such patterns are called minutiae points [21] (Figure 3). Line ends and bifurcations are the most used minutiae points.

<table>
<thead>
<tr>
<th>Minutiae Point</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Line end (termination)</td>
<td>Bifurcation</td>
</tr>
<tr>
<td>Lake</td>
<td>Independent Ridge</td>
</tr>
<tr>
<td>Point or Island</td>
<td>Spur</td>
</tr>
<tr>
<td>Bridge</td>
<td></td>
</tr>
</tbody>
</table>

Figure 4: Types of minutiae points.

Other types (Figure 4) are not so commonly accepted since it is harder to establish minutiae point type automatically.

Minutiae points are described by $x$ and $y$ coordinates, angle between line direction and horizontal axis (Figure 5).

Although minutiae points contain large amount of information about fingerprint, additional information may be extracted from the fingerprint.

Figure 5: Characteristics of minutiae points.

1.2.4 Fingerprint matching

Fingerprints are compared in a process that is called fingerprint matching. Extracted minutiae points from one fingerprint are compared to minutiae points from the other fingerprint and similarity score between two
fingerprints is determined [14]. Fingerprint matching is a difficult task: fingerprints may be distorted [5], rotated or translated; images may contain different parts of the same fingerprint; fingertip skin may have imperfections such as scratches and wounds, image may be noisy or dirt may be left on fingerprint scanner.

1.2.5 Fingerprint classification
In the process of identification a fingerprint is compared to all fingerprints in a database. If fingerprint database is large, the process may become very time consuming. To make it faster, fingerprint classification may be used. Fingerprint class is determined based on the number and location of singular points and only fingerprints of the same class are compared. Commonly 5 classes are used (Arch, Tented Arch, Left loop, Right Loop and Whorl (Figure 6).

![Figure 6: Types of fingerprints.](image)
Arch type fingerprints do not have any singular points. Tented arch type fingerprints have two singular points: core and delta (delta is below core). Loop type fingerprints also have two singular points: core and delta. Delta point is located to the right (in case of left loop) or to the left (in case of right loop) relative to core point. Whorl type fingerprints have two core and two delta singular points. Ridge frequency and orientation maps (Figure 7) are commonly used to evaluate fingerprint type automatically. Ridge frequency map displays local ridge frequency and can also be used to separate foreground from background.

1.2.6 Extraction of fingerprint features
Fingerprint features are extracted in feature extraction process. Typical extraction algorithms use following image processing routines to extract fingerprint features: segmentation (to remove background), normalization (to stretch contrast), binarization (to distinguish ridges and valleys), skeletonization (to make ridges thinner), and detection of minutiae points.
1.2.7 Fingerprint recognition performance evaluation

Biometric systems store biometric information (features) in the form of template that characterizes a person. In case of fingerprints a template is a file that keeps record of singular and minutiae points that were extracted from a fingerprint image. The templates are stored in a database. During verification input template $I$ from a person is compared to a stored template $T$ and similarity score $s(T,I)$ is computed. Similarity score shows the probability that templates $T$ and $I$ come from the same person. Null and alternate hypotheses are:

$H_0: I \neq T$, input template does not come from the same person as in stored template $T$;

$H_1: I = T$, templates $I$ and $T$ are from the same person.

The associated decisions are:

$D_0$: person is not who he claims to be;

$D_1$: person is who he claims to be. To make a decision, similarity score is compared to a threshold $t$. If similarity score is larger than threshold $t$, the decision is made that templates $I$ and $T$ come from the same person ($D_1$). Two types of error may occur:

Type I: false acceptance ($D_1$ is decided when $H_0$ is true);

Type II: false rejection ($D_0$ is decided when $H_1$ is true).

False Acceptance Rate (FAR) is the probability of type I error, False Rejection Rate (FRR) is the probability of type II error:

$$\text{FAR} = P(D_1|H_0 = \text{true});$$

$$\text{FRR} = P(D_0|H_1 = \text{true}).$$

To evaluate the performance of a biometric system on a specific database, similarity score distribution $p(s|H_1 \text{ is true})$ must be collected on templates from the same person (genuine similarity distribution), and distribution $p(s|H_0 \text{ is true})$ on templates that come from different persons (impostor similarity distribution). Figure 8 demonstrates FAR and FRR for a given
threshold \( t \). It is evident, that FAR is a percentage of impostor pairs whose matching score is greater than or equal than threshold \( t \) and FRR is a percentage of genuine pairs whose similarity is less than threshold \( t \). Actually FAR and FRR a functions depending on \( t \). Threshold \( t \) is a tradeoff between FAR and FRR. If threshold is increased, FAR decreases (system becomes more secure), but at the same time FRR increases making it harder for a person to be successfully identified. Additionally to FAR and FRR functions more simple performance indicators are used:

Equal error rate (EER) is an error at such threshold \( t \) that FAR and FRR for that threshold are equal.

Zero FRR is the lowest FAR at which no false rejections are made.

Zero FAR is the lowest FRR at which no false acceptances are made.

To compare different biometric systems FAR and FRR are computed for all thresholds from 0 to maximum and a point \((\text{FAR}(t), \text{FRR}(t))\) is plotted on a graphical plot for each threshold \( t \). The obtained curve demonstrates how FAR depends on FRR for all possible thresholds is called receiver operating characteristic (ROC) curve (Figure 9). ROC curve can be used to analyze such biometric system parameters as FRR at given FAR (For example \( \text{FRR} @ \text{FAR} = 0\% \), \( \text{FRR} @ \text{FAR} = 0.1\% \), \( \text{FRR} @ \text{FAR} = 0.01\% \) or FRR at any other FAR). The lower the ROC curve is, the better is the recognition performance. Although ROC curve does not provide information about confidence intervals, this problem is not significant since the number of impostor and genuine pairs is very high even for small databases since each template in a database is verified against all other templates. If a database consists of 1500 records (15 persons each having 10 fingers scanned 10 times), the number of pairs is \( 1500(1500-1)/2 = 1124250 \).
1.3 Voice Biometrics

1.3.1 Speaker identification and verification tasks

Identification and verification concepts are the same as in fingerprint biometrics.

In verification the comparison 1:1 (“one to one”) is done, that is: a person claims his identity and then the presented speech utterance is compared with an earlier recorded speech examples belonging to the claimed identity. If similarity of the two utterances exceeds a chosen threshold the person’s identity is approved / verified; otherwise the person’s identity is not verified.
Verification problem naturally arises in access control systems as in border or immigration control services.

Any verification algorithm can make two types of errors: some percent of genuine utterances may be rejected (not verified) and some percent of speech utterances belonging to different persons may be claimed as being genuine (belonging to the same person). The first type of error is called False Rejection Rate (FRR) and the second is called False Acceptance Rate (FAR).

These two errors depend on chosen similarity threshold – higher thresholds produce larger FRR and smaller FAR, and inversely the lower thresholds produce smaller FRR but larger FAR. Graph of the parametric curve $x(t) = FAR(t), \ y(t) = FRR(t)$, where parameter $t$ is the similarity threshold, is called Detection Error Tradeoff (DET) curve. DET curve provides visual representation of speaker verification algorithm performance. The lower is the DET curve, the better is the quality of speaker verification algorithm. DET curve is similar to a ROC curve that is commonly used in fingerprint biometrics. The difference in the name appeared when fingerprint biometrics and voice biometrics communities started using different names for the same concept.

In identification comparison 1:$N$ (“one to many” or “one to $N$”) is performed, that is: a person does not claim his identity and the problem is to find the most similar speaker among database of $N$ speakers or more generally sort $N$ speakers in order of similarities to the speech utterance under investigation. Person identification by voice has applications in criminology or in security services (when for example, a mobile phone is recorded and individuals that take part in conversations should be identified).

If there is no some additional information, the $N$ voices are arranged according similarities of $N$ pairs of speech utterances where a pair consists of voice sample under investigation and one of $N$ voice samples that are recorded in a voice database. The pair with the largest similarity gives
hypothesis about identity of speaker whose voice sample is under investigation. There are two subtypes of identification problems that are called open and closed set problems. In the case of the open problem it is not known whether the voice under investigation is contained in the voice database of \( N \) speakers. In the case of closed set identification it is known that one and only one voice sample is contained in a database of \( N \) records. Identification problem with closed set is easier – the pair of voice records with the biggest similarity can be identified as belonging to the same person. In the case of open identification the similarity threshold must be chosen to make a decision whether a voice under investigation is contained in the set of \( N \) voice records. In such case verification is equivalent to a particular case of speaker recognition with open set when \( N = 1 \).

To estimate the quality of speaker identification or other biometric identification systems a ranking curve is used. Ranking curve is a plot for closed speakers set identification. In abscissa axis numbers from 1 to \( N \) are plotted and in ordinate axis the cumulative percentage of speakers that were identified in \( n \)th or smaller place is plotted. For example let \( N = 5 \) and 20 speakers were identified. Let suppose that according to voices similarity 11 speakers were identified in the 1st place, 4 in the 2nd, 3 in the 3d, 0 in 4th and rest 2 in the 5th place. Than ranking curve for the given experiment of speaker identification would be plotted using the points: (1, 55), (2, 75), (3, 90), (4, 90), (5, 100).

1.3.2 Text-dependent and text-independent speaker recognition

Another criterion for classification of speaker recognition systems is the text that is used to recognize a person. If the spoken text is known in advance and the same text is contained in a recorded database of speech utterances and the same phrase is spoken during verification or identification process than the process it is called text-dependent speaker recognition. For example if a person says “I am engineer Jonas Jonaitis, my identity number is 273” at
entrance and the same text is saved in utterances data base, speaker recognition problem is text-dependent. Such recognition systems are used more frequently in verification and require much shorter speech utterances for speaker recognition. However text-dependent and even text-prompted access control systems can be broken down by recorded examples of a person speech utterance. A variation of text-dependent recognition may be used when several different phrases of the same speaker are recorded in utterances database and voice recognition system randomly asks to pronounce a particular phrase during verification. Such systems belong to the so called text-prompted systems and give additional flexibility to the speaker verification process [60]. In the more general case a text-prompted system can ask to pronounce any unknown in advance text.

In text-independent speaker recognition spoken and stored phrases have different text content. Text-independent speaker recognition problem naturally arises when we have a database of speech utterances of suspected persons and a particular phrase or phrases recorded during phone call or by a hidden microphone. One can remember recent examples of questionable Bin Laden records where decision about speaker identity was done under text-independent conditions. It is clear that speech utterances saved in speech database should be sufficiently rich to cover possible phonetic range. If in text-dependent speaker recognition requirement to a phrase duration is about 10 sec., text-independent recognition requires speech examples 3-5 min. long.

Techniques that estimate text-dependent and text-independent speech utterances use different approaches. In text-dependent speech recognition systems Dynamic Time Warping (DTW) technique [61], [62] dominates. DTW technique gives an elegant solution for compensation of variations in speed with which the same phrase is pronounced. In speaker recognition using text-independent speech examples Gaussian Mixture Model (GMM) [63], Vector
Quantization (VQ) [64], Arithmetic Harmonic Sphericity measure (AHS) [65], and different variations of Hidden Markov Model (HMM) [66] dominate. Text-independent recognition systems have an additional source of information that is used in speaker recognition. This source is statistics of phonemes of diphones used in free speech examples. The phonemes statistic can be accumulated manually or using speech to text engines.

1.3.3 Speaker modeling techniques
A general structure of speaker recognition algorithms is presented in the following scheme. For more detailed description of each step of the scheme an overview on modern techniques that are used for speaker recognition was used [67].

A typical scheme of speaker recognition system.

1.3.3.1 Speech signal processing, features
Any speech signal is first pre-emphasized. Pre-emphasizing filter enhances high frequencies of the speech signal spectrum. The pre-emphasizing filter is defined by the following formula:

\[ y(t) = x(t) - ax(t - 1). \]

The value of a parameter \( a \) is taken from the interval \([0.95, 0.99]\) and depends on sampling rate of the speech signal. Some authors use signal
adaptive $\alpha$ values that depend on the contents of a frame. If features are extracted using filter-banks or all-pass filters that have increasing resolution with increase of frequency, application of pre-emphasizing filter is not necessary. In general simple experiments with different $\alpha$ values give empirical answer to optimal $\alpha$ value. If pre-emphasizing gives only a small increase in speaker recognition it is recommended not to apply this filter for the speech signal. The initial speech signal is divided in frames and analysis is done locally by applying a window to overcome boundary problem. A windowed local speech signal is called a *speech frame* or just *frame*. Duration of a frame is 20-30 milliseconds. The frames can have overlap and two neighboring frames can be shifted in time 10 milliseconds back or forward. These values are found empirically and are justified by an average physical duration of time interval when the speech signal is approximately stationary. In theory the shorter the frame the more stationary it is, however it would be difficult to estimate the spectral content of a very short speech frame. 20 milliseconds duration allows estimating spectrum up to 100 hertz that is sufficient for speaker recognition.

The Hamming and the Hanning windows are the most frequently used for frame windowing. Both windows suppress boundary values that increases signal-to-noise ratio in spectrum domain. The fast Fourier transform (FFT) [68], [69] of the windowed signal represents the spectral content of the frame. To apply FFT the samples of a frame should be padded by zeros to have total number of samples that is a power of 2 (for example 256 or 512).

### 1.3.3.2 Mel Cepstrum

The modulus of the FFT represents power spectrum of the frame. The FFT spectrum has a lot of fluctuations that can be reduced by application of a filter-bank series. A fixed representative of the filter-bank averages FFT power spectrum around central frequency. Standard deviation of the smoothing filter increases with rise of central frequency that fits physiological property of
our hearing system. The parameters of the spectrum smoothing filter are
defined by their left, central, and right frequency. Filter can by triangular or
exponential type. In effort to copy the properties of our hearing system many
authors use the Bark/Mel scale for the central frequencies of the smoothing
filters. The central locations of the Mel scale are defined by the following
formula:

\[ f_{Mel} = 1000 \log_2 \left( 1 + \frac{f}{1000} \right). \]

The presented formula is taken from [70]. More complicated versions of the
Mel scale exist but all formulas have a following property: for low frequencies
\( f \) (up to 1000) Mel scale converts frequency almost linearly and for high
frequencies the conversion becomes logarithmic.

Finally, the decimal logarithm is taken of this spectral envelope and is
multiplied by 20 in order to obtain the spectral envelope in decibels (dB). This
tradition comes from electronic engineers who use dB as a standard measure
unit. After this stage of the processing, a vector of features that encodes
spectral content of the frame is obtained. However such features have
redundant information and an additional transformation is performed to
reduce feature dimensionality. The cosine discrete transform is usually
applied here to produce cepstral coefficients [71], [72]:

\[ c_n = \sum_{k=1}^{K} S_k \cos \left( n(k - 0.5) \frac{\pi}{K} \right), n = 1, 2, ..., N. \]

Here \( K \) is the number of power spectrum values \( S_k \) smoothed on Mel scale
central frequencies and \( N \leq K \) is the number of cepstral coefficients.

**1.3.3.3 Linear prediction**

In all-pole Linear Prediction (LP) model \( x_n \) value of a signal is predicted by a
linear combination of its previous values [73]:

\[ x_n = - \sum_{k=1}^{p} a_k x_{n-k} + G e_n, \]
where $p$ is the order of LP model; $a_k$ are linear prediction coefficients (LPC) of the model; $G$ is a gain scaling factor and $e_n$ is the source for the present input. The LPC parameters of LP approximation $\hat{x}_n = -\sum_{k=1}^{p} a_k x_{n-k}$ are found by minimization of a sum of the squared approximation errors.

Traditionally the LP source is not modeled in speaker recognition that limits the use of fundamental frequency to recognize speaker. This limitation can be overcome by modeling of the source or by direct estimation of the fundamental frequency and their statistics.

The LP model leads to the transfer function

$$H(z) = \frac{G}{1 + \sum_{k=1}^{p} a_k z^{-k}} = G / A(z),$$

where $A(z)$ is inverse filter of the $p$-th order of all pole LP model. Mean square error of the residuals $x_n - \hat{x}_n = \epsilon_n$ is typically minimized because this leads to more simple linear equations for the prediction of the coefficients that are easily solved by computers.

Figure 10 illustrates the spectrum of Lithuanian vowel “a” estimated by three different methods. The black curve gives the FFT power spectrum, green curve represents modulus of transfer functions estimated by LP model of order $p=8$ and the blue curve correspond to the power spectrum estimated by LP model of order $p=16$. In general FFT spectrum is over-detailed and the modulus of the transfer function of LP model gives an envelope of FFT spectrum and the resolution of the envelop is controlled by the order $p$ of the LP model.
Figure 10: Wave function of the Lithuanian vowel "a" (above) and its spectrum estimated by different methods (below).

1.3.3.4 LPC-based cepstral parameters

Coefficients of fixed order LP model are estimated for any speech frame. LPC parameters are rarely used directly for speaker recognition. The prediction coefficients are unstable in case of small perturbations of speech signal and do not have a simple interpretation. It was discovered that some linear combinations of the LP coefficients can give approximations of the cepstral coefficients. If the order $p$ of the LP model tends to infinity the approximations tends to equalities [74].
The linear expressions that convert LPC to LP Cepstral Coefficients (LPC to LPCC) are the following:

\[
\begin{align*}
    c_0 &= \ln G, \\
    c_m &= a_m + \sum_{k=1}^{m-1} c^k_m c_k a_{m-k}, 1 \leq m \leq p, \\
    c_m &= \sum_{k=1}^{m-1} c^k_m c_k a_{m-k}, p < m.
\end{align*}
\]

1.3.3.5 Additional transformations

Mel or LP Cepstral Coefficients allow a simple procedure for channel compensation. Channel distortions can be modeled as additional filter that is applied to the signal. Since the channel filter is approximately constant in time and the cepstral coefficients correspond to the Fourier coefficients of the logarithm of the power spectrum, the channel transfer function transforms into an additional term which may be removed by subtracting mean values of the cepstral coefficients. This operation is named cepstral mean subtraction (CMS) and is often used to increase the tolerance of speaker recognition to channel differences, differences in recording conditions, background noise, etc. However CMS do not solve such problem as additional noise which has no convolutive property. A partial solution for reduction of additive noise problem can be equalization of variance of each cepstral component.

Cepstral coefficients do not contain information about dynamics of the speech. For that purposes the so called delta (\(\Delta\)) and delta-delta (\(\Delta\Delta\)) parameters are added to cepstral coefficients. The delta and delta-delta parameters are an approximation of first and second derivatives of the cepstral coefficients as functions in time [75]. The derivatives can be estimated by the following formulas:

\[
\begin{align*}
    \Delta c_m &= \frac{\sum_{k=-l}^{l} k c_{m+k}}{\sum_{k=-l}^{l} |k|}, \\
    \Delta\Delta c_m &= \frac{\sum_{k=-l}^{l} k^2 c_{m+k}}{\sum_{k=-l}^{l} k^2},
\end{align*}
\]
where $c$ with upper index $m$ represents vector of cepstral coefficients of the $m$-th frame and parameter $l = 1, 2$ or $3$. The first component of vector of cepstral coefficients $c_0 = \ln G$ is not invariant to recording conditions and is not included into features set; however the first component of $\Delta$ and $\Delta\Delta$ vectors becomes invariant to the level of loudness of recording device and can be included into final features vector.

1.3.4 Models of Speakers and their matching

When speech utterance is represented as a sequence of feature vectors it is called that features of the signal are extracted. To have possibility to compare extracted features the same type of features are selected for target (database) and for investigative (input) speech examples. However different utterances may have different textual content, different duration and therefore cannot be compared directly frame-by-frame. In this section a short introduction to feature matching techniques is provided. Two groups of measures that are used for estimation of speech utterances are known. The first group constructs a statistical model for measured features vectors. If features $f$ are $K$ dimensional vectors a density function $d = d(f)$ that maximizes likelihood of observed features of the frames is constructed. If at authorization process a speech frame with features vector $f$ is observed, direct substitution of $f$ to $d(f)$ gives likelihood of that frame for the target speaker with the density function $d = d(f)$. Such substitutions should be done for each frame and an average $d(f)$ value represents similarity measure of the two speakers models. Much faster comparison of the two voice samples can be done by constructing a density function for investigative (input) voice record also and estimating the probability that two densities correspond to the random source of features vector $f$. Another type of measures directly compares pairs of features vectors that correspond to different frames of the target (database) and investigative (input) voice and a global measure of similarity is constructed from local comparisons of
similarity of pairs of frames. This technique is called template matching, it is more intuitive, and in common, is more expensive. Both types of measures have their merits and demerits, and therefore a combination of them is often used.

1.3.4.1 Template Models
In the most simple template model only a single template \( f \), which is the model target (database) speech record, is used. Template \( f \) belongs to the linear space of all possible feature vectors and can be defined as mean vector of feature vectors of speech frames. Such approach minimizes mean square Euclidean distance error between a fixed template and all frame feature vectors. If we have \( f^m, m = 1, 2, ..., M \) feature vectors of \( M \) frames of a target voice record, then target speaker template would be

\[
\bar{f} = \frac{\sum_{m=1}^{M} f^m}{M}.
\]

Distance between feature vector \( f^m \) of an investigative (input) \( m \)-th frame and target model \( f \) is expressed by:

\[
d(f^m, \bar{f}) = \sqrt{(f^m - \bar{f})^T W (f^m - \bar{f})}.
\]

Here \( W \) is a feature components weighting matrix. Euclidean distance is defined by identity matrix, covariance matrix of frame feature vectors define Mahalanobis distance. If initial feature vectors are transformed to the space which basis consists of orthogonal eigenvectors of the covariance matrix, the Mahalanobis distance is equal to Euclidean distance and computational cost of the latter is much smaller (proportional to the dimensionality of feature vector) [76].

1.3.4.2 Dynamic Time Warping
If speaker recognition is text-dependent or text-prompted with vocabulary covered in saved speech records database, template matching is an intuitive approach and often used in speaker recognition. The idea is that even the
same phrases are pronounced by the same person, they sound more similar than phrases pronounced by different speakers. Voice recognition is easier if speakers cooperate with authorization system and pronounce personalized utterances such as “I am Jonas Jonaitis, engineer, my personal number 375” and “I am Petras Petraitis, my job position is in support division, personal number 781”. It is natural to expect that average value of frame-to-frame distance of both records of the same has good discriminative characteristic for recognition of the claimed speaker. However in text-dependent and text-prompted case small variations in speed by which utterances are spoken appear. Dynamic Time Warping (DTW) [62] gives an elegant solution which in some sense optimally arranges the frames that should by paired to compare two utterances. The cost of DTW algorithm is moderate since distances between all frames of two utterances should be estimated that makes complexity quadratic. Suppose we have \( \{f^1, f^2, \ldots, f^M\} \) input voice features vectors and \( \{\bar{f}^1, \bar{f}^2, \ldots, \bar{f}^L\} \) target voice features vectors. Than DTW algorithm gives non-decreasing set of indices \( j(1), j(2), \ldots, j(L) \in (1, 2, \ldots, M) \) that minimizes with some additional conditions the average distance

\[
d(f, \bar{f}) = \sum_{m=1}^{M} \frac{d(f^m, \bar{f}^{j(m)})}{M}.
\]

Figure 11: Frame correspondences without alignment (left) and with DTW alignment (right).

Figure 11 illustrates identical alignment \( j(m) = m \) of frames of two curves that have the same number of points (left part) and the one which minimizes
average distance between two curves (right part). Some attempts to explore DTW method for text-independent speaker recognition are known, but since DTW algorithm has quadratic complexity and text-independent speech records are much longer than text dependent records, application of DTW technique in such cases is limited.

1.3.4.3 Vector Quantization approach

The main drawback of DTW template matching approach is that this technique does not work for text-independent speaker recognition. A direct on templates matching of two speech samples would be estimation of distances or similarities between all possible pairs of features vectors that correspond to two speech utterances and minimization of the obtained distances matrix by columns and rows and calculation of average minimal distances. However such direct approach leads to big computational cost. For example if we have two utterances 3, 5 minutes long with length and distance between neighboring frames of 10 milliseconds, the total number frame pairs similarity of which should be estimated will be 3x60x10 x 5x60x10 = 54 e 6 that is sufficiently big number even for modern computers. Vector Quantization is an old well known technique which allows reducing initial number of vectors by rounding them to centroids that contain the so called codebook [98]. Vectors of codebook are usually formed by some clustering procedure. The size of the codebook ranges in speaker recognition from 32 to 2048 and has tendency to grow recently. Let $C$ denote the codebook constructed for target speaker vectors. Then the average quantization distance of investigated voice feature vectors defines distance between the two speakers. Formally for the distance such expression is used:

$$d(f, \bar{f}) = \sum_{m=1}^{M} \frac{\min_{\bar{f} \in C} d(f^m, \bar{f})}{M}.$$
The vector quantization technique reduces computational costs and is often used as one of similarity/distance measure for voice comparison. To further increase the speed of comparison of two voice records, the features vectors of both vectors can be quantized and distances or similarities between code words of the two vector codebooks can be used. However such approach decreases the quality of speaker recognition. Sometimes such double quantization approach is used for initial selection of most similar pairs of records that are further investigated by traditional Vector Quantization modeling.

1.3.4.4 Nearest Neighbors method

Nearest neighbors (NN) method combines strength of DTW and VQ methods. Unlike the VQ method, NN method keeps all features vectors of the target data [98]. For each input frame the most similar enrolled target frame is found and for each enrolled target frame the most similar input frame is found and the two series of minimal distances are averaged. This method is the most computationally complex but it gives the best results in of text-independent speaker recognition when the recognition is done by template matching methodology.

1.3.4.5 Stochastic models

Template methods work well for text-dependent speaker recognition however they are computationally complex expensive and not state of the art quality when text-independent recognition is needed. In stochastic approach a density function that maximizes the likelihood to observe the same feature vectors for input phrases that are observed for target speakers is constructed. For each target speaker a separate density function is constructed. Then the estimation of the likelihood to observe feature vectors of unknown speaker for all target models gives the measure of probability that the unknown input speaker has the same identity as a target speaker. So we have set of
conditional probability distribution functions with the number of conditions equal to the number of target speakers. Conditional probability density function (pdf) of a target speaker is estimated from the set of training features vectors and can be parametric on non-parametric. In any case (parametric or non-parametric pdf) probability that feature vectors of unknown speaker are generated by the claimed target model can be estimated. This probability gives not normalized matching scores. To build parametric model, a specific form of pdf should be assumed and then free parameters of the model are determined by maximization of likelihood of observed training features vectors. One possible assumption can be made that the pdf is the multivariate normal density function. Then free parameters of the model would be mean vector $\mu$ and covariance matrix $C$ of the multivariate normal distribution. In this case value

$$p(f^m | \text{target model}) = \sqrt{2\pi}^{-K} |C|^{-\frac{1}{2}} \exp\left(-\frac{1}{2} (f^m - \mu)^T C^{-1} (f^m - \mu)\right).$$

Here $K$ is dimension of frame features vector, $|C|$ is determinant of the covariance matrix. Having features training vectors $\bar{f}^l, l = 1, \ldots, L$, mean vector and covariance matrix of target model can be estimated by the following expressions:

$$\mu = \frac{\sum_{l=1}^L \bar{f}^l}{L},$$

$$C = \frac{\sum_{l=1}^L (\bar{f}^l - \mu) \cdot (\bar{f}^l - \mu)^T}{L - 1}.$$

Here “•” denotes point-wise multiplication. However multivariate normal distribution is a very simple approximation of real training vectors and therefore Gaussian Mixture Model (GMM) in which density function is a normalized sum of a few different multivariate normal distributions is used. More detailed description of this model is given in next chapter. Although strictly speaking speech frames do not provide independent feature vectors it is assumed that they are independent. Such assumption allows estimating
conditional probability of unknown speaker simply by multiplying frames probabilities.

Another very popular stochastic model is Hidden Markov Model (HMM) [97]. Hidden Markov Model is a double embedded stochastic process in the sense that the stochastic process is not directly observable. The HMM is defined by:

1. Finite set of states $s_i, i = 1, ..., N$,
2. $N \times N$ matrix of transition probabilities $a_{i,j}$, which means “transit at next time moment to the state $j$ if we were at state $i$ at current time”. It is assumed that transition probabilities do not depend on time.
3. Finite set of $M$ observable symbols $v_m$,
4. $N \times M$ matrix of probabilities $b_{j,m}$ which means “probability to observe symbol $v_m$ at state $s_j$”,
5. $N$ probabilities $\pi_j$ that define state probabilities at initial moment.

Having observations set and HMM it is easy to calculate probability of such observation. However in practice HMM should be constructed from observations. For fixed parameter $N$ the rest of HMM parameters and sequence of states are chosen by maximizing probability to have the observations set under the model and the states sequence.

These two problems are solved using Baum-Welch and Viterbi algorithms 98.

1.3.4.6 Gaussian Mixture Model

The most popular stochastic model that is successfully applied for many years in speaker recognition is Gaussian Mixture Model (GMM). The authors of this method are Reynolds and Rose [80]. In this model, pdf function is modeled by the expression:

$$p(f \mid \text{target model}) = \sum_{i=1}^{I} p_i g_i(f),$$

where $g_i(f) = \sqrt{2\pi^{-K}} |C_i|^{-\frac{1}{2}} \exp \left( -\frac{1}{2} (f - \mu_i)^T C_i^{-1} (f - \mu_i) \right)$.
is shifted multivariate normal distribution and  

\[ p_i \geq 0, i = 1, \ldots, I, \sum_{i=1}^{I} p_i = 1 \]

are weights of the shifted and scaled normal distributions. The complete Gaussian mixture density has \( I \) mean \( K \) dimensional vectors, \( K \times K \) covariance matrices and positive weights. However, it is often assumed that covariance matrices have simple structure, for example diagonal, that save memory required for model and simplifies the estimation of the model. GMM model has simple interpretation. Speech signals are composed by different phonemes that can by clustered in feature space and each component of GMM density can represent a particular phoneme and the weights of mixture represents frequency/probability of occurrence of that phoneme. Mean vectors \( \mu_i \) define acoustic positions of the phonemes and covariance matrices \( C_i \) sharpness of localization of phonemes around their acoustic centre. GMM has advantage over VQ approach since the latter can be interpreted as an approximation of pdf by a discrete histogram with centers in code words. On the other hand, code words of VQ can be used for initial positions of mean vectors \( \mu_i \) that are later tuned by an iteration process that maximizes a posteriori probability to observe training features vectors.

Let \( \lambda = (p_i, \mu_i, C_i), i = 1, 2, \ldots, I \), represents parameters of the GMM. Than having target training features vectors \( \bar{f}^l, l = 1, \ldots, L \), the GMM parameters are found by maximizing the a posteriori probability

\[ p(\bar{f}^l | \lambda) = \prod_{l=1}^{L} p(\bar{f}^l | \lambda) . \]

The a posteriori probability highly non-linearly depends on the model parameters that require applying some iterative process for maximization of the probability. Having constructed GM target model the measure of correspondence of unknown voice to the target voice is estimated by

\[ p(\bar{f} | \lambda) = \prod_{m=1}^{M} p(f^m | \lambda) , \]

where \( f^m \) are feature vectors of unknown speaker voice utterance.
1.3.5 Speaker recognition by Lithuanian authors

The most contribution to speaker recognition is done by Antanas Leonas Lipeika with co-authors. In his and J. Lipeikiene first paper [81] speaker identification problem is considered. In [82] a modification of VQ method for speaker identification is proposed. The main contribution was in modification of quantization algorithm that allowed increasing codebook by one and tune it for optimization of speaker identification quality. In [83] a notion of pseudo stationary segments was proposed and applied for speaker recognition. Pseudo stationary segments were found by joining adjacent frames that have similar spectral content. Similarities of spectral contents were estimated by likelihood ratio distance [84]. When pseudo stationary segments are found, a direct minimization of a likelihood distance is done for fixed segments of investigative (input) voice versus all possible target (database) segments and, vice versa, pseudo stationary segment of target voice is fixed and the most similar to that segment investigative segment is found. Average values of likelihoods of the pseudo stationary signals are used as final similarity measure. In [85] an idea of application of LPC residual signal to increase the quality of speaker recognition was proposed. It was shown that fusion of ordinary speaker similarity measures with the ones estimated for LPC residual signal can increase speaker recognition quality. In this paper usual Euclidean metrics calculated on LPC derived cepstral coefficients were investigated and likelihood ratio distance was mentioned. It was shown that for both metrics an increase in speaker recognition quality after fusion of the two types of feature metrics is observed. In [86] the possibilities of DTW based techniques for speaker recognition were investigated. In [87] the details of GMM were analyzed and a compact set of features that are estimated on the base of Line Spectral Pairs (LSP) that are derived from marginal LPC variations was proposed. It was shown that dimensionality of features can be reduced two or more times compared to a conventional cepstral features without significant
loss in speaker recognition quality. Another work worth mentioning is [88], where the usage of consonant-vowel diphones for speaker discrimination was proposed.

1.4 Problem Relevance

It is easy to notice that biometric technologies are spreading across the world. Even low cost notebooks and mobile phones have integrated fingerprint scanners and users can log on with fingerprint instead of password. Integrated webcams are used to identify a person by face, and microphones are used to provide access to the system by the voice. All these technologies provide faster and reliable access to data, bank account or computer than password, because passwords can be stolen, forgotten, lost or unlocked by specific software. These are the reasons why many universities, companies and institutions invest time and money in research and development of biometric algorithms.

Several international competitions were arranged to compare different biometric algorithms and track progress in biometric research: FVC (FVC 2000, FVC 2002, FVC 2004, FVC 2006 and FVC ongoing), NIST (National Institute of Standards and Technology) MINEX (MINEX, MINEX II and Ongoing MINEX) and PIV for fingerprints; NIST Face Recognition Vendor Tests (FRVT) for faces; NIST Speaker Recognition Evaluation (SRE) for voice biometrics; NIST Iris Challenge Evaluation (ICE), Independent Testing of Iris Recognition Technology (ITIRT) for irises are the largest and most known biometric competitions. These competitions show that in spite the progress in such aspects as reliability, speed and interoperability is impressive, there are many difficult problems left to overcome.

All biometric technologies are dependent on input quality: If obtained fingerprint image is noisy, low contrast or deformed; recorded voice phrase is of low volume or very short, iris image is obstructed by eyelids, reflections or glasses, face image is acquired in poor lightning conditions or using low
quality camera, the task of verification becomes more difficult. The main challenge of modern biometric algorithms is to overcome these difficult conditions and extract as much data as possible. Innovative methods help algorithm developers better understand the weaknesses of their algorithms and address them. Algorithm developers have to take into consideration that when the popularity of biometric technology increase, requirements to algorithm accuracy also increase. Error rate of one percent may be suitable for a small company using time attendance system based on biometrics, but will make a lot of problems to a bank with millions of customers or during elections to prevent multiple voting.

This work is about fingerprint and voice biometrics. Fingerprint biometrics is the most popular biometrics: fingerprint scanners are cheap, easy to use and the process of verification is fast.

Voice biometrics is the most available biometrics, because no additional hardware is needed. Most computers have audio interface with possibility to plug microphone, microphones are integrated into webcams, headphones and mobile phones.

1.5 Research Objects
The thesis research objects are: performance evaluation of fingerprint extraction algorithm using fingerprint synthesis, fingerprint matching method that is able to match deformed fingerprints, person identification using voice and fusion of both biometrics.

1.6 The Objectives and Tasks of the Research
The aim of the research was to complexly analyze research area and address difficult problems. In the first part of the work fingerprint extraction algorithm development problems are analyzed and fingerprint image synthesis is suggested to overcome that problems. In the second part of the work fingerprint matching algorithm problems are analyzed and new matching
algorithm is proposed to deal with them. New person identification by voice method is addressed in the third part of the work and multibiometrics using fingerprints and voice is proposed to increase identification accuracy.

1.7 Scientific Novelty
The new method of fingerprint image synthesis is introduced in first chapter. Differently from already existing synthesis methods it can generate fingerprint images with predefined features. Such images with known characteristics allow evaluating the performance of fingerprint extraction algorithm independently from fingerprint matching algorithm. A new practical application for synthetic fingerprints is suggested: they can be used to estimate the quality of images in a given database or the quality of a fingerprint scanner.

New fingerprint matching algorithm that is described in the second chapter does not perform fingerprint registration (evaluation of rotation and translation) and is capable to match fingerprints with elastic deformations.

Multibiometrics using new person identification by voice method and new fingerprint matching method is described in next chapters. The performance was analyzed using specially prepared multibiometric database.

This work is the first attempt to prove that there is no correlation observed between similarities based on fingerprints and similarities based on voice. Such independence of two biometrics means that they can be successfully combined into multibiometrics.

1.8 Practical Importance of the Work
Methods described in this work can be used to solve many difficult tasks. Fingerprint image synthesis (chapter 2) can be used to generate large fingerprint databases, to evaluate the performance of fingerprint extraction algorithm. Since it is possible to generate a fingerprint image with pre-defined properties and features, it becomes easy to evaluate such properties of
fingerprint extraction algorithm as stability to noise and accuracy of extracted features.

New fingerprint matching method (chapter 3) allows accurate matching of plain and rolled fingerprints with elastic deformations that are common in rolled fingerprints and sometimes occur in plain fingerprints.

Multibiometrics using fingerprints and voice (chapters 4 and 5) can provide more flexible and accurate way of person identification.

1.9 Approval of Research Results

Research results were published in valuable international journal Informatica. The conference papers were presented and an oral presentation in INFORMATION TECHNOLOGIES (IT2010) conference was done.

1.10 Defended propositions

1. New fingerprint image synthesis method can generate fingerprints with predefined features. Such fingerprints can be used to test and develop biometric systems.

2. Fingerprint image synthesis uses iterative convolution with large kernel that is a very time consuming operation. An optimization that speeds up synthesis process several times was presented.

3. A method to evaluate the performance of fingerprint extraction algorithm using synthetic fingerprints can be used evaluate extractor’s performance.

4. Fingerprint matching method that does not perform fingerprint registration and is able to match deformed plain and rolled fingerprints with better accuracy.

5. New speaker identification method outperforms traditional speaker identification methods.
6. Since fingerprint and voice similarities do not correlate much, multibiometric using both fingerprints and voice can further increase identification accuracy.

1.11 Publications

International journals which are included into the International Master Journal List (ISI):


International journals which are included in the Scientific Master Journal Proceeding List (ISI):


Journal submissions under review:


1.12 Outline of the Thesis

The thesis consists of 3 main parts: fingerprint biometrics (chapters 2 and 3), voice biometrics (chapter 4) and multibiometrics (chapter 5).
The 2nd chapter describes fast fingerprint image synthesis method that can be used to create large fingerprint databases and to evaluate the performance of fingerprint extraction methods. The 3d chapter is devoted to a fingerprint matching method that is robust to deformations and does not perform fingerprint alignment. The 4th chapter introduces the use of group delay features of linear prediction model for speaker recognition. The 5th chapter presents multibiometrics using fingerprints and voice. The 6th chapter completes thesis with brief summary and conclusions. At the end of the work a bibliography list is presented.

2 Fingerprint image synthesis

This chapter presents a fingerprint synthesis method that can generate a fingerprint with predefined minutiae points. Fingerprint type is chosen randomly and singular points positions and quantities are chosen randomly according to the fingerprint type. Orientation map is generated using fingerprint orientation model. Ridge frequency map is generated. Initial image with drawn minutiae points that are oriented by orientation map is constructed. Iterative filtering of the initial image with Gabor filters that are oriented using orientation map and constructed using frequency map produces fingerprint image with minutiae points located at the predefined positions. An optimization of the iterative filtering is described. Synthetic fingerprint images are used to evaluate extraction algorithm's stability to noise. A measure of extraction algorithm's robustness to noised fingerprint images is proposed.

2.1 Introduction

Much attention is being paid to different biometric algorithms such as person identification by unique features. Fingerprint identification is one of the most
popular ways to identify a person and much research is done in this area of biometrics. Identification process consists of fingerprint image acquisition, feature extraction and feature matching. Different methods to evaluate algorithm performance are proposed [38], [39], [40], [41] and most of them use fingerprint databases such as NIST SD4 [42] or NIST SD14 [43] to calculate accuracy. Features are extracted in enrollment phase [44], [45] and then extracted features are matched against each other in matching phase [13] [18] [46] to calculate Receiver Operating Characteristic (ROC), Detection Error Trade-off (DET) or other statistics [47]. Many competitions [18], [48] have been arranged to analyze and benchmark different commercial and academic algorithms. The biggest and most thorough of them was NIST arranged competition MINEX [49]: Vendors could send their extraction or matching algorithms and best extractors and matchers were selected. Majority of vendors send both algorithms and it is interesting, that in many cases matching algorithms performed better with extractors from the same vendors (it can be seen from scenario 1 in MINEX report [49]). It can be easily explained, since many vendors develop both matcher and extractor and they know about typical problems of their extractors and can compensate for them in matching phase. It is hard to develop an accurate extraction algorithm because it is hard to evaluate it without a good matcher and since most vendors develop both algorithms, they are not sure that even if performance of their matcher or extractor is good enough, it will be good when used with other extractor (or matcher).

Estimation of biometric algorithms performance expressed in ROC or DET curves depends on database of fingerprint images, quality of extraction and quality of matching algorithm. To have the possibility to estimate extractor and database quality separately from matching routine, we propose to utilize synthesized fingerprints images. Synthesized images can serve as a reference or as an ideal database that allows introducing some quantitative quality
measures for estimation of extractor’s performance for a particular database. If one extractor is applied on several fingerprint image databases, the database quality can be associated with the proposed quality measure. The situation is similar to situation when the quality of several extraction algorithms can be compared if same database for each extractor is used to calculate statistics.

The ROC and DET characteristics of extracting algorithm can be replaced by a quality measure that accounts information about exact positions, types and orientations of minutiae. To have fingerprints images with predefined minutiae points, we extend SFINGE fingerprint image synthesis method [50].

2.2 SFINGE

Different synthesis methods were analyzed [50], [51], [52] and SFINGE [50] was chosen as a base method. It is well described and its ability to generate finger-like images was tested in fingerprint verification competitions (FVC2000 [38] FVC2002 [18] FVC2004 [48] and FVC2006), in which one of four databases was generated synthetically. Generated fingerprints look like real ones, and identification algorithms performance is similar to performance obtained on real fingerprints.

SFINGE (Synthetic Fingerprint Generation) consists of several steps:

Fingerprint form generation, fingerprint type and orientation map generation, density map generation, ridge generation.

2.2.1 Fingerprint form

Fingerprint generation is starting by fingerprint form determination. Fingerprint form can be described by many different methods. For example, it can be described by an ellipse, or by a square with rounded corners. SFINGE method uses five coefficients, which can be generated randomly, or inserted manually or derived from the real fingerprint (Figure 12).
2.2.2 Fingerprint type and orientation map

These properties are strongly related, because fingerprint type depends on positions of singular points (cores and deltas), and positions of singular points depend on orientation map. Different methods of orientation map generation are described in literature [53], [54] and any of them can be used to generate fingerprint orientation map with greater or smaller accuracy. Sherlock-Monroe [53] method was chosen in this work because of its simplicity. Fingerprint orientation map is calculated in following steps:

1. Fingerprint type is selected (manually or randomly);
2. Quantities of singular points are selected depending on fingerprint type. Positions of all singular points (loops and deltas) are selected (randomly or manually) with restrictions that depend on chosen type.
3. Having loops and deltas quantities and positions, orientation map is generated by the following formula:

$$\theta = \frac{1}{2} \left[ \sum_{i=1}^{N_d} \arg(z - ds_i) - \sum_{j=1}^{N_c} \arg(z - ls_j) \right].$$

where $z$ is a complex number made from $(x, y)$ coordinates of point, in which orientation $\theta$ is calculated; $N_d$ – number of delta type singular points; $N_c$ – number of core type singular points; $ds_i$ – complex number made from
\(i\)-th delta coordinates; \(ls_i\) – complex number made from \(j\)-th loop coordinates; \(arg\) – complex number argument;

Orientation is calculated in each pixel of fingerprint image (Figure 13).

![Figure 13: Example of orientation maps for different type fingerprints.](image)

### 2.2.3 Ridge density map generation

Ridge density map is generated using following information about fingerprint characteristics: Default distance between ridges is 9 pixels (here and below we assume that scanner’s resolution is 500 pixels-per-inch (DPI)), ridge frequency is lower on the top of the image, and lower on the bottom [20].

### 2.2.4 Ridge generation

Ridges are generated by iterative filtering of the blank image (initial image) with random dots, by Gabor filter [55] that is created using orientation and density from orientation and density maps:

1. Black image with white dots in random positions is generated,
2. Image is filtered several times with spatial (Gabor) filter (Figure 14), which has orientation and frequency properties. Filter is generated by the following formula:

\[
h(x, y; \lambda, \theta, \psi, \sigma, \gamma) = \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right) \cos\left(2\pi\frac{x\psi}{\lambda} + \psi\right),
\]

\[
x_{\theta} = x \cos \theta + y \sin \theta,
\]

\[
y_{\theta} = -x \sin \theta + y \cos \theta.
\]
In this equation, $\lambda$ represents the wavelength of the cosine factor, $\theta$ represents the orientation of the normal to the parallel stripes of a Gabor function, $\psi$ is the phase offset, $\sigma$ is the sigma of the Gaussian envelope and $\gamma$ is the spatial aspect ratio, and specifies the ellipticity of the support of the Gabor function.

![Gabor filter](image)

Figure 14: Gabor filter.

Orientation and frequency values are taken from orientation and frequency maps.

Filter is applied to entire initial image, and after several iterations random dots begin to grow into the lines and lines begin to form fingerprint ridges. Ridges fill the image and minutiae points (ends and bifurcations) appear (Figure 15).

![Ridge generation](image)

Figure 15: Ridge generation from initial image. Filtered images are shown in the top row, and binarized versions are in the bottom row.
2.2.5 Analysis
An algorithm was implemented, and after experiments and research it was modified to generate minutiae points not in random positions, but in predefined ones. The following section describes a method that is fast and can generate images with minutiae in given positions.

2.3 Modified SFINGE Method
Since method is based on SFINGE method, steps like orientations map calculation and filtration are not described here once more. This section is focused on the differences between original and modified method.

Main steps of fingerprint generation are:
1. fingerprint type is chosen (randomly or manually);
2. orientations (Figure 13) are generated;
3. Gabor filters of orientations that present in orientations image are generated before filtering to speed up generation;
4. initial image is constructed;
5. initial image is filtered with Gabor filters that are oriented by orientation image.

![Initial image construction steps](image.jpg)

Figure 16: Orients map (left), initial image with drawn minutiae points (center), generated image, with resulting minutiae points marked with circles(right).

Initial image is constructed by the following steps:
1. zero valued image of given size is constructed;
2. coordinates (positions) and types of minutiae points are generated randomly or selected manually;
3. small images of minutiae are drawn on the initial image in the selected positions so that minutiae orientations are aligned with orientation map.

There are two types of minutiae points – line ends and bifurcations. Since these types are invertible (line end is a bifurcation on the inverted image), a bifurcation is drawn using positive (+1) value pixels, and line end is drawn using negative (-1) value pixels (Figure 16 (center)).

The most straightforward way to generate a fingerprint is to filter the Initial image with Gabor filters that are oriented by orientation image (Figure 13), but since responses of Gabor filters are calculated in every pixel, it is a computationally complex operation. An optimization was implemented to perform iterative filtering only in those pixels that are required in current iteration to generate a fingerprint. The main idea of the improvement is to start filtering from positions of drawn minutiae and near it, and to extend filtering area until entire image is generated. For example, if Gabor filter is 10 pixels wide, then in the first iteration pixels that are from 0 to 10 pixels away from the drawn minutiae points are filtered, in the second iteration – pixels that are from 1 to 11 pixels away from drawn minutiae points are filtered, in third iteration – pixels that are from 2 to 12 pixels away from drawn minutiae points are filtered, in fourth iteration – from 3 to 13 pixels away, and so on, until the fingerprint is generated (no pixels are left to filter). To perform fast calculation of distances to minutiae points, Euclidean Distance Map (EDM) [56] is calculated from initial image. The EDM map is an image, and value of each pixel indicates the distance to the nearest object (drawn minutiae point). The order of filtering can be easily calculated from EDM. In the first filtering iteration only pixels that have values from 0 to 10 in EDM are filtered, in second filtering iteration only pixels with values from 1 to 11 in Euclidean
Distance Map are filtered in initial image, in third iteration only pixels with values from 2 to 12 are filtered, in fourth iteration – from 3 to 13 and so on. (Figure 17 shows an example)

![Iterations of generation](image)

Figure 17: Iterations of generation. An area that is white is filtered in each iteration.

Filtering is performed by applying Gabor filter (orientation $\phi$ is taken from orientation map, frequency $f$ is taken from the frequency map) to each pixel of the initial image in the order that is calculated from EDM.

Generated image can be noised or transformed after generation to provide it more natural look.

The described optimization speeds up generation process more than 5 times comparing to a straightforward version.

The resulting generation speed is more than 2 fingerprints per seconds on Intel Core 2 Duo 6600 processor.

It can be noticed that though some additional minutiae points appear in result image, all initial minutiae points are present and location, direction and type of them are the same as in the initial image.

Similar synthesis approach was independently used in [57] with the aim to investigate the possibility of fingerprint reconstruction from standard template. The main differences in generation process are summarized in the following table (Table 1):
2.4 Correlation of synthetic fingerprints and real fingerprints

Synthetic fingerprints look like real, but before using them, it must be proved that they have the same properties as the real ones, and can be used instead of them. The generation method is based on SFINGE method, which was validated in [57], but an additional test to further investigate the problem was performed:

- DB1A database (800 fingerprints from 100 individuals) from FVC2002 competition was chosen.
- Features (minutiae points) and orientation maps were extracted from all fingerprints using VeriFinger SDK [23].
- A synthetic fingerprint for each extracted template was generated using modified SFINGE method.
- Templates from each synthetic fingerprint were extracted using VeriFinger SDK.
- Three different matching scenarios were implemented:
  1. synthetic fingerprints vs. real fingerprints;
  2. synthetic fingerprints vs. synthetic fingerprints;
  3. real fingerprints vs. real fingerprints.

In synthetic fingerprints vs. real fingerprints scenario each template from 800 synthetic fingerprints was matched against 800 templates from real fingerprints using matcher described in [13] providing 800 similarity scores (8 genuine scores and 792 impostor scores) for each synthetic fingerprint. Similarity scores were analyzed to determine the rate of successful matches between a synthetic fingerprint and 8 real genuine fingerprints. The match was considered successful, if genuine score is more than maximal impostors score. The process was repeated for second and third scenarios. The results are summarized in the following table (Table 2):

<table>
<thead>
<tr>
<th>Number of matched genuines</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scenario 1: Synth. vs. Real</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>99.625</td>
<td>99.625</td>
<td>99</td>
<td>97.375</td>
<td>89.125</td>
</tr>
<tr>
<td>Scenario 2: Synth. vs. Synth.</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>99.875</td>
<td>99.125</td>
<td>97.125</td>
<td>89.625</td>
</tr>
<tr>
<td>Scenario 3: Real vs. Real</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>99.75</td>
<td>98.875</td>
<td>96.375</td>
</tr>
</tbody>
</table>

The first column (1) shows what the probability that a synthetic (in case of scenario 1) fingerprint has a successful match with at least one real fingerprint from 8 genuine fingerprints is.
The second column (2) shows what the probability that a synthetic (in case of scenario 1) fingerprint has a successful match with at least two real fingerprints from 8 genuine fingerprints.

The third column (3) shows what the probability that a synthetic (in case of scenario 1) fingerprint has a successful match with at least three real fingerprints from 8 genuine fingerprints is.

The last column (8) shows what the probability that a synthetic (in case of scenario 1) fingerprint has a successful match with all real fingerprints from 8 genuine fingerprints.

It can be seen from the Table 1 that each synthetic fingerprint matches successfully with all 8 real genuine fingerprints in 89.125% of cases and up to 3 real genuine fingerprints are matched successfully in 100% of cases.

The probability that a synthetic fingerprint successfully matches with all real genuine fingerprints (scenario 1 column8,) is almost the same as the probability that a synthetic fingerprint successfully matches with all synthetic genuine(scenario 2 column 8) fingerprints.

The conclusion can be drawn that synthetic fingerprints are very similar to real ones and can be used instead of real fingerprints when needed.

2.5 Extraction algorithm performance evaluation

The aim of the extraction algorithm (extractor) is to extract different fingerprint characteristics and properties such as minutiae point’s locations, orientations and types, fingerprint type estimation and so on. Most extraction algorithms (extractors) consist of different image processing algorithms such as image normalization, texture orientation estimation, binarization, skeletonization and ridge frequency analysis. Developers of algorithms have to overcome many problems: source image can be noisy, fingerprint may be with scars and other imperfections, errors made in one extraction step can strongly affect other step, so it is necessary to have some way to evaluate extractor performance and find what errors can be fixed and which steps
need more attention. It would be very useful to have some reference fingerprints, with known characteristics (Figure 18). The output of the extractor could be compared to known characteristics and errors could be calculated. Such task could be done by manual analysis of several real fingerprints with marking all the necessary properties such as minutiae points, fingerprint type, singular points locations and so on, but it is a very time consuming operation and the resulting data will be non-objective (results will depend on person. For example – one fingerprint can have more than hundred minutiae points, and each minutiae point have such characteristics as: location, direction, and type. To evaluate extractor’s performance to a good degree of accuracy one may need to repeat this procedure hundreds or thousands times so it becomes obvious that such work cannot be done manually.

Fingerprint image synthesis can be used to evaluate extractor’s accuracy. For example, many extractors perform orientation map estimation and since orientation map in synthetic fingerprint is generated by a known mathematical model, exact orientation in every pixel is known. It can be compared to an estimated orientation and error can be calculated. Fingerprint type, ridge frequency, minutiae point’s locations, types and directions are all predefined and can be used to evaluate extractor's accuracy. It is possible to generate thousands of fingerprints and evaluate extractor's performance with unprecedented accuracy. Extractor's stability to noise, deformations or scars can also be evaluated by adding artificial noise of different power to generated images and then initial data can be compared to the output of the extractor.
2.6 Experiments

To illustrate how synthetic images can be used to evaluate extractor’s performance, an experiment was done. The method was used to analyze how artificial noise affects extractor’s results. Extractor from NIST certified VeriFinger SDK [23] was chosen.

Three databases were prepared:

1. DB1 - 1000 synthetic fingerprint images with 50 initial minutiae points per fingerprint;
2. DB2 is a publicly available database DB1A from FVC2004 [48] competition (high quality fingerprint images from FBI certified scanner);
3. DB3 is a publicly available database NIST SD29 [33][WSQ compressed fingerprint images from scanned fingerprint cards (only plain fingerprints were used).

The resolution of images in DB2 and DB3 is 500 DPI; resolution of synthetic fingerprint images is about 500 DPI.

Images were noised with shot (‘salt and pepper’) noise [56] - some percent of all image pixels were set white or black. Positions of noised pixels were chosen randomly (Figure 19).
Minutiae points from noised images were extracted and following statistics for each noise density $d$ (percentage of the noised pixels) from 0 to 100 were calculated:

1. percent of initial minutiae points that was found on noised image (Minutiae point was considered as found if it is the nearest minutiae point to the initial minutiae point and the distance to it is less than 10 pixels;

2. how found minutiae positions were affected by noise (the average distance in pixels between initial minutiae and found minutiae).

Since accurate minutiae positions on real databases are not known (as in generated fingers), minutiae points extracted from not noised images were considered as initial minutiae points. Results are presented in following figures:
Figure 20: Quantity of initial minutiae points found on noised images (horizontal axis - noise density from 0% to 100%, vertical axis - quantity of found minutiae from 0 (0%) to 1 (100%).

Figure 21: Average distance between minutiae in noised image and minutiae in initial image (horizontal axis - noise density from 0% to 86%, vertical axis - average distance in pixels.
It can be noticed from the Figure 20 that on DB1 more than 90% of minutiae points are detected up to noise densities around 60% (when more than half of image pixels are corrupted) and the average distance to initial minutiae point is about 1.5 pixels (Figure 21).

On DB2 more than 90% of minutiae are detected if noise density is less than 20% (Figure 20), but the average distance to original minutiae point is still less than one pixel (Figure 21).

On DB3 more than 90% of minutiae are detected only if noise density is less than 5% (Figure 21). At noise density 20% only 60% of minutiae are found and the average distance to original minutiae point is more than one pixel (Figure 21).

Real fingerprint images have lower signal-to-noise ratio because some noise is added during fingerprint acquisition process (dust on scanner, marks from previously scanned fingerprints, digitization errors, image compression artifacts).

We propose to use synthesized image database as references in estimation of quality of the extractor. For example curve of Figure 20 that corresponds to synthetic DB1 is the most right. We postulate that this curve corresponds for ideal scanner or ideal database and has 100% quality. The measure of quality can be defined as $100 \times \frac{S_1}{S_1}$, where $S_1$ is an area below the graph in Figure 20 that corresponds to DB1. Quality of DB2 and DB3 databases or their corresponding scanners is $100 \times \frac{S_2}{S_1}$ and $100 \times \frac{S_2}{S_1}$. Here $S_2$ and $S_3$ are areas below the corresponding graphs in Figure 21. After calculation of the areas, quantitative extractor quality on DB2 and DB3 was calculated. The numbers are 64.7% for DB2 and 35.3% for DB3. Graphs in Figure 20 represent proportion of reliable detected minutiae in respect of added “salt and pepper” noise. Thus the calculated qualities represent extractor quality for the two databases in the sense of quantity of reliably detected minutiae.
Graphs in Figure 21 can be used in the similar manner to estimate precision of extracted minutiae positions. Average error on DB2 is 7.8 times higher than on DB1, on DB3 – 11.1 times higher than on DB1. Note that in both cases extraction qualities for DB3 were lower and this well correlates with published ROC and DET characteristics for these databases [48], [58].

2.7 Summary and Conclusions of the Chapter
A method of fingerprint image generation was described in detail. The method is fast, and can generate images with minutiae points that have predefined properties such as location, direction and type. It can be used not only to generate large databases of fingerprints, but to precisely evaluate extraction algorithm performance and detect its weak sides (stability to noise, scratches, deformations and other imperfections). Experiments show that quality of generated images is much better than quality of real fingerprints and since initial minutiae positions are known, the accuracy of evaluation is higher.

It is common to evaluate database, extractor or matcher accuracy by calculating statistics like ROC on some database, but the result of such evaluation depends on all three components – quality of database, quality of extractor and quality of matcher. When synthetic database is used, evaluation results depend on only two components – quality of extractor and quality of database. Influence of the matcher is eliminated by using synthetic database as a reference. Two measures for extractor’s performance estimation on different DB were introduced. The resulting quality is in the range of 0 and 100%, where 100% corresponds to the case of synthetic images. The obtained numeric values of the qualities correspond to known ROC characteristics of test databases.

The described method can be used to design an extraction algorithm that is more tolerant to scanner noise, fingerprint scratches and deformations. Since
additional minutiae points appear in result image during generation process, additional workaround may be needed to overcome this issue.

3 Fingerprint matching

3.1 Introduction

Most automatic fingerprint verification and identification systems use minutiae information from fingerprints to align and compare images or their templates to speed up the matching process. We refer to minutiae as ridge ending or ridge bifurcation with any additional local features. Extraction of minutiae from fingerprint image is out of the scope of this work.

Much effort has been made to create matching algorithms capable of dealing with distortion and deformations in fingerprint images. Exhaustive overview of possible methods is made in [20] and [21]. Thin-plate spline model is used to deal with distortion in [5]: first, local matching is performed on structures that consist of minutiae and its two closest neighboring minutiae points to determine which minutiae possibly match, then global matching is made to find registration parameters; after finding the global registration parameters that coarsely align two fingerprints, elastic deformation is eliminated using thin-plate spline model, and final match is made. The authors reported major increase in performance. However, their approach uses registration estimation that is not reliable when fingerprints are distorted since accurate registration does not often exist, see Figure 22. Two distorted fingerprints are presented. After registration, only small common part that is not distorted is left.
Figure 22: Two different impressions of the same fingerprint before and after best registration.

Errors in registration lead to errors in further steps. Matching based on local and global structures is described in [24]. Local matching uses local structures that consist of minutiae point and its neighboring minutiae points and is rotation and translation tolerant. Local structures from both fingerprints are matched to find the best matching pair. This pair is used as a reference correspondence point, and other minutiae points are aligned based on this correspondence. After alignment global structure matching is performed. To account for deformation, large bounding boxes are used, but to decrease the probability of false match, the matching certainty level function that provides some sort of match probability instead of just "matched" or "not matched" result is defined. Although authors reported good matching performance, the disadvantages of their matching algorithm are similar to [5]. If the fingerprints are distorted, the exact registration parameters do not exist, and even the reference local pair cannot be used to align them. Errors in choosing the right reference point or incorrect alignment lead to incorrect match. Other methods are described in literature [20], but most of them are either variations of above described methods that use registration, or their computational cost is too high or they use some other, not minutiae methods to deal with distortion and cannot be used with existing fingerprint databases based on minutiae. For example, an interesting method is introduced in [28] where authors normalize the fingerprint image to a canonical form so that ridges are equally spaced and less affected by distortion. In [7] a distortion model that could describe elastic deformation found in fingerprint images is
presented. Authors validated it by manually setting deformation parameters, but no automatic optimization technique that could be used to automatically derive deformation parameters while matching minutiae is known. In general, distortion elimination is a hard problem that could improve performance of most matchers, if properly solved. After normalization or deformation removal a rigid matcher could be used for direct comparison [18]. Another normalization technique was introduced in [14] – the minutiae distance is normalized at the matching stage according to the local ridge frequency. This method could improve matcher performance for good quality fingerprints where reliable frequency estimation is possible, and for minutiae pairs that are not far from one another, so that changes in ridge frequency along the fingerprint that occurs even in not distorted images are less than errors that are made while estimating the frequency.

In this chapter, a completely new approach of minutiae matching is proposed as a framework with broad range of possible implementations. One of the most simple but effective implementation is discussed here. The method consists of three main steps: matching of local structures, correspondence set construction and validation of higher order local structures. The first step has the following properties: Low false rejection ratio (FRR), rotation and translation invariance, locality (for tolerance to deformations) and low computational complexity.

Possible implementation will be discussed in section 3.3. The second step receives a similarity matrix filled with similarity score of every minutiae point from the first template compared with every minutiae point from the second template. In spite of the fact, that one minutiae point from the first template can be very similar to several different minutiae points from the second template, every minutiae point can make only one correspondence between the templates. Construction of minutiae correspondence set is discussed in section 3.3.2. While constructing the minutiae correspondence set no
information about the global fingerprint structure is used. The last step of global fingerprint structure validation is discussed in section 3.4.

3.2 Fingerprint Matching Without Global Alignment
This chapter is about a method of minutiae based fingerprint matching that is robust to deformations and does not perform fingerprint alignment. It concentrates on comparing rotation and translation invariant local structures defined by minutiae point and its neighboring minutiae points. Then the collection of most probable correspondences of matched minutiae is found. Finally, the local structures of higher order are validated. All three steps are completely rotation and translation invariant, robust to nonlinear deformations and do not use any fingerprint alignment. Experimental results on publicly available as well as internal databases showed an improved performance of the proposed method in comparison with the traditional minutiae based algorithms that perform fingerprint registration.

3.3 Local Matching
In most general case, template of fingerprint is the description of minutiae points set. Two sets of minutiae must be compared while matching two fingerprints. For simplicity, we will call $T$ (test set) – the first set of $N$ minutiae and $S$ (sample set) – the second set of $M$ minutiae. The order of sets is not important because the proposed method is symmetric. We define local matching as a comparison of $N$ local structures from set $T$ to $M$ local structures from set $S$ where every local structure is associated with minutiae which serves as a reference point to that local structure. The result of local matching step is a $N \times M$ similarity matrix filled with similarities between local structures.

3.3.1 Local Structure
Generally, local structure could be anything from a minutiae point identified by a vector starting at $(x, y)$ and local ridge direction $\varphi$ to a set of minutiae
with some portions of original image. However, we are looking for a structure that is rotation and translation invariant, local (for tolerance to deformations) and easy comparable.

One of possible candidate could be the structure that we define using graph notation similar to [24], see Figure 23. The local structure associated with the minutiae $m_i$ (defined by a vector starting at $(x_i, y_i)$ and local ridge direction $\varphi_i$) for distance $d_{\text{max}}$ and maximum number of nearest neighbors $n_{\text{max}}$ is the graph $S_i = (V_i, E_i)$ consisting of:

$$V_i = \{ m_j | \text{distance}(m_i, m_j) < d_{\text{max}} \}, |V_i| \leq n_{\text{max}};$$

$$E_i = \{ e_{ij} | e_{ij} \text{ connects } m_i \text{ and } m_j \},$$

where $e_{ij}$ is labeled with tuple $(i, j, \text{distance}(m_i, m_j), \phi_{ij}), \phi_{ij}$ is the angle between $m_i$ and $m_j$ directions. Additionally, other features can be used to improve the performance.

Such local structure is rotation and translation invariant and tolerant to non-rigid nonlinear deformations.

![Figure 23: Local structure associated with minutiae $m_i$.](image)

3.3.1.1 Similarity Score

In spite of the fact, that minutiae extraction from fingerprint image is out of the scope of this work, possible errors of false detected and missed minutiae cannot be ignored. The local structures cannot be compared directly if any of these errors is present. To deal with these errors we construct a similarity function $CS(S_i^T, S_j^S)$ for comparison of two local structures $S_i^T$ and $S_j^S$ from test and sample fingerprints. If there were no extraction errors the
edges of every local structure could be sorted in clockwise (or counterclockwise order) starting from the direction of associated minutiae and compared directly by a function:

\[
CS(S^*_j,S^s_j) = \sum_{k=1}^{|e^*_i|} CE(e^*_i, e^s_j),
\]

\[
CE(S^*_j,S^s_j) = \begin{cases} 
0, & \text{if } \Delta d \geq \Delta d_{\text{max}} \text{ or } \Delta \phi \geq \Delta \phi_{\text{max}}; \\
\frac{\Delta d_{\text{max}} - \Delta d}{\Delta d_{\text{max}}} + \frac{\Delta \phi_{\text{max}} - \Delta \phi}{\Delta \phi_{\text{max}}}, & \text{otherwise.}
\end{cases}
\]

\[
\Delta d = |\text{distance}(m^*_i, m^*_j) - \text{distance}(m^s_i, m^s_j)|,
\]

\[
\Delta \phi = \min(|\phi_i - \phi_j|, 2\pi - |\phi_i - \phi_j|),
\]

\[
\Delta d_{\text{max}}, \Delta \phi_{\text{max}} - \text{thresholds, } w_d, w_\phi - \text{predefined parameters.}
\]

However, we can deal with errors introduced by extraction in the following way:

1. Sort \( E^*_i \) edges in a clockwise order (starting from the direction of associated minutiae) into a sequence \( Ev^*_i \);
2. Sort \( E^s_j \) edges in a clockwise order (starting from the direction of associated minutiae) into a sequence \( Ev^s_j \);
3. Find the longest common subsequence (LCS) of \( Ev^*_i \) and \( Ev^s_j \) using the same similarity function CE from (3.2) for comparison of sequence elements.
4. Sum up the similarities of edges that make the longest common subsequence:

\[
\overline{CS}(S^*_j,S^s_j) = \sum_{e^*_i, e^s_j \in LCS(Ev^*_i, Ev^s_j)} CE(e^*_i, e^s_j).
\]

As a convenient abuse of terminology we will use \( CS \) instead of \( \overline{CS} \) to represent similarity between two local structures.

### 3.3.2 Correspondence Set Construction

After calculating similarity between every local structure from test and sample fingerprints similarity matrix \( SM_{N \times M} \) is filled with these values. This
matrix can be used to construct a correspondence set of minutiae pairs where every local structure belongs maximum to one correspondence:

\[ C = \{(S^T_i, S^S_j) | S^T_i \in T, S^S_j \in S\}, |C| \leq \min(N, M). \]  \hspace{1cm} (3.4)

Though many different approaches can be used to find minutiae correspondence set, a maximum weighted matching on bipartite graphs is used to find the correspondence set maximizing the sum of similarities between local structures.

Bipartite graph is constructed from similarity matrix with vertices defined by local structures from both fingerprints and weighted edges defined by greater than 0 similarities between associated local structures. We use Hungarian algorithm [59] to solve this problem in \( O (\max (N, M)^3) \) time in worst case.

### 3.4 Validation

Until a correspondence set is constructed no global fingerprint registration is used and for robustness to deformations it will not be used anywhere in the proposed method. Although local structures from test and sample fingerprints can have high similarity they can be located differently in respect to each other in fingerprints (see Figure 24).
Similar cases should be taken under consideration. The easiest solution would be to perform global alignment of fingerprints, but since global registration is not used, local structures of higher order are constructed to control how local structures are located in the fingerprint. We define structures of higher order $HS_{ij}^T$ and $HS_{ij}^S$ as pairs of local structures from the correspondence set that was constructed in previous section for test and sample fingerprints:

\[
HS_{ij}^T = (c_i^T, c_j^T), \quad 1 \leq i < j \leq |C|, \\
HS_{ij}^S = (c_i^S, c_j^S), \quad 1 \leq i < j \leq |C|.
\]  

(3.5)

Local structures of higher order $HS_{ij}^T$ and $HS_{ij}^S$ are rotation and translation invariant. Additionally, they hold information on how local structures are situated in the fingerprint in respect of each other without a need of global fingerprint registration. Some of the local structures of higher order are marked in Figure 24 by Latin letters $a$, $b$, and $c$. For example, structure $b$ (identified by local structures 1 and 3, angles $\alpha$ and $\beta$, and distance between minutiae points associated with local structures) from Figure 24 in test fingerprint is compared to corresponding structure $b$ in sample fingerprint. If
the structures are not consistent they are not used in calculating similarity score between fingerprints.

### 3.4.1.1 Similarity Score

We define similarity score $SS$ between two local structures of higher order $HS_{ij}^T$ and $HS_{ij}^S$ as:

$$SS(HS_{ij}^T, HS_{ij}^S)$$

$$= \begin{cases} 
0, & \text{if } \Delta l \geq \Delta l_{\text{max}} \text{ or } \Delta \alpha \geq \Delta \alpha_{\text{max}} \text{ or } \Delta \beta \geq \Delta \alpha_{\text{max}}; \\
\frac{w_l}{\Delta l_{\text{max}}} + w_\alpha \frac{\Delta \alpha_{\text{max}} - \Delta \alpha}{\Delta \alpha_{\text{max}}} + w_\beta \frac{\Delta \alpha_{\text{max}} - \Delta \beta}{\Delta \alpha_{\text{max}}}, & \text{otherwise.}
\end{cases} \quad (3.6)$$

$m_i^T, m_i^S, m_j^T, m_j^S$ – minutiae points associated with local structures from $HS_{ij}^T$ and $HS_{ij}^S$,

$\Delta l = |\text{distance}(m_i^T, m_j^T) - \text{distance}(m_i^S, m_j^S)|$,

$\Delta \alpha = \min(|\alpha^T - \alpha^S|, 2\pi - |\alpha^T - \alpha^S|)$,

$\Delta \beta = \min(|\beta^T - \beta^S|, 2\pi - |\beta^T - \beta^S|)$,

$\alpha^T, \alpha^S, \beta^T, \beta^S$ – angles between the segments connecting the local structures of higher order and directions of their associated minutiae,

$\Delta l_{\text{max}}, \Delta \alpha_{\text{max}}, w_l, w_\alpha$ – predefined parameters.

### 3.5 Final Similarity Score

We define similarity score between two fingerprints as a sum of similarity scores between all local structures of higher order (that passed a validation step) combined with similarity scores of local structures that make them:

$$\text{SCORE} = \frac{\sum_{i,j} f(SS(HS_{ij}^T, HS_{ij}^S), CS(S_i^T, S_i^S), CS(S_j^T, S_j^S))}{g(N, M)}, \quad (3.7)$$

where $S_i^T, S_i^S, S_j^T, S_j^S$ are local structures that make $HS_{ij}^T$ and $HS_{ij}^S$,

$f \left( SS(HS_{ij}^T, HS_{ij}^S), CS(S_i^T, S_i^S), CS(S_j^T, S_j^S) \right)$ can be one of the following (but not limited to):

$$SS(HS_{ij}^T, HS_{ij}^S) + \frac{1}{2} \left( CS(S_i^T, S_i^S) + CS(S_j^T, S_j^S) \right); \quad (3.8)$$

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\[ g(N,M) \text{ function is used to normalize similarity score for differently sized fingerprints.} \]

Selection of the most suitable \( f \) and \( g \) functions can improve matching performance in cases when fingerprints of different sizes are compared. \( f(x,y,z) = x \times y \times z \) and \( g(x,y) = x \times y \) were used in this work together with (3.9) equation.

### 3.6 Evaluation of threshold parameters

#### 3.6.1 Threshold Parameters in Local Structures

Two threshold parameters are used in constructing local structures: \( d_{\text{max}} \) and \( n_{\text{max}} \). Experimental results show that changing value of parameter \( d_{\text{max}} \) hardly changes matching performance. However, to make structures more local the value of 150 pixels was chosen. Additional testing was performed on several databases for choosing the value of \( n_{\text{max}} \) parameter. It showed that \( n_{\text{max}} \) is a tradeoff between speed and quality. The value of 10 was chosen. The results are shown in Figure 25.
3.6.2 Threshold Parameters in Similarity Functions

The proposed method uses several predefined thresholds ($\Delta d_{\text{max}}, \Delta \varphi_{\text{max}}, \Delta l_{\text{max}}, \Delta \alpha_{\text{max}}$), however we show that similarity functions are constructed to be robust. None of them uses a hard decision (see (3.2), (3.6), and (3.7)) because the information on level of similarities is lost in that way. Our similarity functions include this information and are stable in respect to varying values of threshold parameters. Actually, these parameters control what amount of deformation is allowed by the proposed method. For example, allowing stronger deformations (higher thresholds values) results in higher false acceptance rates but lower false rejection rate. The parameters we used ($\Delta d_{\text{max}} = 12$, $\Delta \varphi_{\text{max}} = 17^\circ$, $\Delta l_{\text{max}} = 12$, $\Delta \alpha_{\text{max}} = 17^\circ$) was a compromise between FAR and FRR. However, additional testing showed that the chosen values can be changed within $\pm 50\%$ without noticeable impact to the performance of the proposed method.
3.7 Performance Evaluation

The complexity of the algorithm consists of three main stages: local structure matching, correspondence set construction and validation. The complexities of the stages when number of features in first fingerprint is \( N \) and in the second fingerprint is \( M \) are: \( O(N \cdot M) \), \( O(\max(N, M)^3) \), \( O(\min(N, M)^2) \) respectively, that gives resulting complexity of the algorithm:

\[
O(N \cdot M + \max(N, M)^3 + \min(N, M)^2) = O(\max(N, M)^3).
\]

The performance of the proposed method was tested on publicly available NIST Special Database 29 [33] fingerprint database (hereafter referred as SD29). The database consists of 216 ten-print fingerprint card pairs with both the rolled and plains scanned at 19.7 pixels per mm. For direct comparison we chose publicly available NIST fingerprint image software NFIS2 [34] minutiae based fingerprint matching algorithm (hereafter referred as BOZORTH3). Fingerprint minutiae extractor from NFIS2 (MINDTCT) was not used in the evaluation because of big number of false minutiae it produces (BOZORTH3 matcher uses only 150 minutiae of best quality from the fingerprint template to deal with this problem). We tested the proposed matching method with commercially available fingerprint minutiae extraction algorithm of better quality [23] (hereafter referred as COMM). We will refer to the proposed method as Local Structure Matcher (LSM) in all experiments.

SD29 database consists only of fingerprint images that were scanned from fingerprint cards. Additional tests were done to prove that the proposed method works well with live scanned fingerprints. The following databases were chosen:

1. DB1 from FVC2002 fingerprint verification competition [18] collected with optical sensor "TouchView II" from Identix. The database consists of 800 different fingerprints with 8 impressions per finger;
2. DB2 from FVC2002 fingerprint verification competition collected with optical sensor optical sensor "FX2000" from Biometrika. The database consists of 800 different fingerprints with 8 impressions per finger;

3. Neurotechnology’s internal database collected with optical single-finger scanner "DFR 2090" from Identix (hereafter referred as INTERNAL1). The database consists of 1400 different fingerprints with 10 impressions per finger;

4. Neurotechnology’s internal database collected with high-quality optical single-finger scanner "Cross Match Verifier 300" (hereafter referred as INTERNAL2) recommended for large scale automatic fingerprint identification systems. The database consists of 1400 different fingerprints with 10 impressions per finger.

5. A relative comparison with other algorithms that perform registration can be found at: http://bias.csr.unibo.it/fvc2006/

3.8 Results
NIST VTB fingerprint system with Bozorth98 matcher (previous version of BOZORTH3) participated in Fingerprint Vendor Technology Evaluation (FpVTE) 2003 [36] and proved to be comparable to other commercial algorithms and even better than almost half of the contestants. The following experiment shows an improvement of the proposed method over BOZORTH3 matcher with COMM minutiae extractor. 18 ROC curves were calculated on different parts of SD29 [35] (P2P – plain vs. plain fingers, P2R – plain vs. rolled fingers, R2R – rolled vs. rolled fingers, RT – right thumb, LT – left thumb, RI – right index, LI – left index, RM – right middle, LM – left middle) of SD29 for both methods. The results (False rejection rate – FRR when false acceptance rate – FAR is 0.01%) are shown in Table 3 and Table 4.
Table 3: COMM+BOZORTH3 FRR @ FAR = 0.01% on different parts of SD29

<table>
<thead>
<tr>
<th>part</th>
<th>RT</th>
<th>LT</th>
<th>RI</th>
<th>LI</th>
<th>RM</th>
<th>LM</th>
<th>average</th>
</tr>
</thead>
<tbody>
<tr>
<td>P2P</td>
<td>7.1</td>
<td>6.2</td>
<td>18.9</td>
<td>15.0</td>
<td>14.8</td>
<td>14.1</td>
<td>12.68</td>
</tr>
<tr>
<td>P2R</td>
<td>12.7</td>
<td>12.8</td>
<td>14.7</td>
<td>18.6</td>
<td>14.6</td>
<td>12.2</td>
<td>14.27</td>
</tr>
<tr>
<td>R2R</td>
<td>16.3</td>
<td>11.3</td>
<td>6.6</td>
<td>5.9</td>
<td>8.3</td>
<td>6.0</td>
<td>9.08</td>
</tr>
</tbody>
</table>

Table 4: COMM+LSM FRR @ FAR = 0.01% on different parts of SD29.

<table>
<thead>
<tr>
<th>part</th>
<th>RT</th>
<th>LT</th>
<th>RI</th>
<th>LI</th>
<th>RM</th>
<th>LM</th>
<th>average</th>
</tr>
</thead>
<tbody>
<tr>
<td>P2P</td>
<td>7.14</td>
<td>9.89</td>
<td>14.8</td>
<td>11.5</td>
<td>15.9</td>
<td>13.2</td>
<td>12.07</td>
</tr>
<tr>
<td>R2R</td>
<td>4.95</td>
<td>7.69</td>
<td>4.4</td>
<td>6.59</td>
<td>5.49</td>
<td>8.79</td>
<td>6.318</td>
</tr>
</tbody>
</table>

The proposed method improves FRR at FAR = 0.01% from 12.01% to 9.20% on average. As expected, the largest improvement was gained on rolled-to-rolled fingerprint matching were stronger deformations of fingerprints are possible.

Figure 26 and Figure 27

Figure show the performance of the proposed method on live scan fingerprints from FVC2002 databases that were collected with optical scanners.

Figure 26: COMM+BOZORTH3 compared to COMM+LSM on FVC2002 DB1 database.
Summary of improvements (FRR @ FAR = 0.01%) over all databases is presented in Table 5.

Table 5: FRR @ FAR = 0.01% on tested databases with commercial minutiae extractor

<table>
<thead>
<tr>
<th>Database</th>
<th>BOZORTH3</th>
<th>LSM</th>
</tr>
</thead>
<tbody>
<tr>
<td>SD29 (average)</td>
<td>12.01</td>
<td>9.20</td>
</tr>
<tr>
<td>FVC2002 DB1</td>
<td>8.73</td>
<td>3.29</td>
</tr>
<tr>
<td>FVC2002 DB2</td>
<td>5.82</td>
<td>3.00</td>
</tr>
<tr>
<td>INTERNAL1</td>
<td>5.65</td>
<td>2.3</td>
</tr>
<tr>
<td>INTERNAL2</td>
<td>1.78</td>
<td>0.44</td>
</tr>
</tbody>
</table>

The largest improvement was achieved for the live scanned fingerprints.

False rejection rate (FRR) at 0.01% FAR is up to 4 times (one-tailed paired t-test; p < 0.0005; Table 5) lower comparing with BOZORTH3 matcher.

3.9 Summary and Conclusions of the Chapter

A framework to match deformed fingerprints was presented in this chapter. It consists of simple and intuitive steps. The proposed implementation of the steps is straightforward and flexible, does not use registration, and is capable of matching deformed fingerprints. It leaves much freedom in combining the suggested methods with other approaches. Evaluation of algorithm was made
on large data sets with different matching parameters. It has been shown that proposed method is flexible and tolerant to rotation, translation and deformation of fingerprint images. Performance of the method was compared with BOZORTH3 matcher and improvements up to 4 times (one-tailed paired t-test; p < 0.0005; Table 5) in false rejection rates at 0.01% FAR were demonstrated.

4 Speaker Recognition

4.1 Introduction

New text independent speaker identification method is presented. In this chapter. Phase spectrum of all-pole linear prediction (LP) model is used to derive the speech features. The features are represented by pairs of numbers that are calculated from group delay extremums of LP model spectrum. The first component of the pair is an argument of maximum of group delay of all pole LP model spectrum and the second is an estimation of spectrum bandwidth at the point of spectrum extremum. A similarity metric that uses group delay features is introduced. The metric is adapted for text independent speaker identification with general assumption that test speech channel may contain multiple speakers. It is demonstrated that automatic speaker recognition system with proposed features and similarity metric outperforms systems based on Gaussian mixture model with Mel frequency cepstral coefficients, formants, antiformants and pitch features. Automatic speaker recognition quality still remains pretty low in comparison with other biometric identification methods based on fingerprints [13], irises and even faces analysis [26] [30]. Conventionally, the front-end of the recognition system uses features such as cepstral, Bark or Mel frequency cepstral coefficients [4]. The features are based on spectrum amplitude of the speech frames or their residual parts of linear prediction model [16][15]. In
our opinion mainstream of speaker recognition algorithms underestimate information contained in phase spectrum. The idea that spectrum phase can contain valuable information for speaker recognition is not very surprising because it is known that traditional power spectrum resonant characteristics can be derived exclusively from the phase spectrum [11], [22]. To resolve stability problem, the phase spectrum of traditional Linear Prediction (LP) model is used. In [32] the group delay features for speaker recognition were derived directly from the Fourier spectrum of the speech frames. Such approach requires special techniques dealing with instabilities of unwarped Fourier spectrum. We combine [11] and [37] techniques to extract group delay features of LP model. In [11] third order derivatives of the LPC phase spectrum were used to extract speech formants. We explore only first and second derivatives of LPC phase spectrum. The zero-crossings of the second derivative provides information about formants positions. LPC phase first derivative at formants frequencies gives simple approximations of the formants bandwidth. In [37] a connection between LPC phase and Line Spectrum Frequencies (LSF) is described. That inspired us to construct a symmetrized form of LPC phase representation which saves features computation cost and gives simple formulas for approximation of LPC spectrum poles. Gaussian Mixture Model (GMM) (see [25], [11]) becomes a standard technique for modeling of distributions of speakers features and their comparison. Since our features are restricted to the rectangle \((0, \pi) \times (0, 1)\) we estimated features distribution using histogram technique and constructed an information theory based similarity measure for comparison of speech utterances.
4.2 Group Delay Features of all-pole LP model

4.2.1 Linear Prediction

In Linear prediction (LP) model [10] samples of a speech frame are represented in the form

\[ x_n = \sum_{i=1}^{P} a_i x_{n-i} + G e_n, \]  

(4.1)

where \( a_1, a_2, ..., a_p \) are the Linear Prediction Coefficients (LPCs), \( P \) is the model order, \( G \) and \( e_n \) are the excitation gain and source, respectively. The LPCs are derived adaptively for each 20-30 ms speech frame by minimization of excitation mean square energy. For simplicity, we will assume that the order of LP model is uneven, i.e. \( p = 2M - 1 \). The LPC spectrum or the transfer function of the LP filtering is defined by:

\[ H_z = \frac{G}{A(z)}, \]  

(4.2)

where

\[ A(z) = 1 - \sum_{i=1}^{2M-1} a_i z^{-i}. \]  

(4.3)

is the inverse filter. The LPC spectrum represents an envelope of the speech spectrum.

4.2.2 Phase of Spectrum of LP model

Let us define symmetrical polynomial \( p(z) \) and antisymmetrical polynomial \( q(z) \) by the formulas:

\[ p(z) = \frac{z^M A(z) + z^{-M} A(z^{-1})}{2}, \]  

(4.4)

\[ q(z) = \frac{z^M A(z) - z^{-M} A(z^{-1})}{2i}, i = \sqrt{-1}. \]  

(4.5)

The \( p(z) \) and \( q(z) \) polynomials are related to the symmetrical polynomial \( P(z) \) and \( Q(z) \) of Line Spectrum Frequencies (LSF) analysis [37] by the following formulas:
\[ P(z) = A(z) + z^{-2M} A(z^{-1}) = 2z^{-M} p(z), \quad (4.6) \]
\[ Q(z) = A(z) - z^{-2M} A(z^{-1}) = 2iz^{-M} q(z). \quad (4.7) \]

On the unit circle \( p(z) \) and \( q(z) \) are real-valued,

\[ |A(z)|^2 = p(z)^2 + q(z)^2, \quad (4.8) \]
\[ p(z) + q(z)i = z^M A(z). \quad (4.9) \]

The equations (4.8) and (4.9) show that the frequency response and the phase of the transfer function of the LP model satisfy the equations:

\[ |H(z)| = \frac{G}{\sqrt{p(z)^2 + q(z)^2}}, \quad (4.10) \]

and

\[ (\arg H(e^{i\omega})) = \Phi(\omega) = M \omega - \arctan\left(\frac{q(e^{i\omega})}{p(e^{i\omega})}\right), \quad \omega \in [0, 2\pi), i = \sqrt{-1}. \quad (4.11) \]

### 4.2.3 LPC Phase Spectrum Features

The LPC spectrum in the all-pole representation has the following form:

\[ H(z) = \frac{G}{\prod_{m=1}^{p} (1 - r_m e^{i\alpha_m z^{-1}})} \quad (4.12) \]

where \( r_m e^{i\alpha_m} \) is location of the \( m \)-th pole of the LPC spectrum, and \( \alpha_m \in [0, 2\pi) \) is the angular frequency of the pole. From Eq. (4.12) follows that the \( m \)-th pole contributes to the LPC phase spectrum with the additive term

\[ \arctan\left(\frac{r_m \sin(\omega - \alpha_m)}{1 - r_m \cos(\omega - \alpha_m)}\right). \]

Therefore for the first and second phase spectrum derivative we have:

\[ \frac{d\Phi(\omega)}{d\omega} = \sum_m \frac{r_m \cos(\omega - \alpha_m) - r_m}{1 - 2r_m \cos(\omega - \alpha_m) + r_m^2}; \quad (4.13) \]
\[ \frac{d^2\Phi(\omega)}{d\omega^2} = -\sum_m \frac{r_m (1 - r_m^2) \sin(\omega - \alpha_m)}{(1 - 2r_m \cos(\omega - \alpha_m) + r_m^2)^2}. \quad (4.14) \]

The negative derivative of phase of the LP spectrum is called group delay of LP model. The poles locations are not estimated and the phase spectrum
derivatives are calculated by numerical differentiation of Eq. (4.11) identity to reduce calculation time.

Equation (4.13) gives that for the strong pole with \( r_m \) close to 1 one can expect local maximum of the group delay at a point \( \omega_m \) close to the angular frequency \( \alpha_m \). The local maximum \( \omega_m \) can be found as second derivative zero-crossing point which is closest to the \( \alpha_m \). (4.13) gives:

\[
\Phi'(\omega_m) \approx \frac{r_m}{1 - r_m}
\]

and

\[
r_m \approx \frac{\Phi'(\omega_m)}{1 + \Phi'(\omega_m)}
\]

Considering the provided observations, we define the group delay features of a speech frame as a set of pairs

\[
\left( \omega_m, \frac{1}{1 + \Phi'(\omega_m)} \right) = (\omega_m, \delta_m),
\]

where \( \{\omega_m\} \) is the set of all zero crossings of the phase spectrum second derivative that belong to the radian frequency interval \((0, \pi)\) and

\[
\delta_m = 1 - \frac{\Phi'(\omega_m)}{1 + \Phi'(\omega_m)} = \frac{1}{1 + \Phi'(\omega_m)}
\]

defines a bandwidth of a formant of the speech frame.

### 4.3 Speech Utterance Similarity Measure for Speaker Identification

Suppose there are two sampled speech utterances \( \{x_n\} \) and \( \{y_n\} \) and similarity between them must be measured. Let's assume that \( \{x_n\} \) samples belong to a speaker \( X \) of the training set and \( \{y_n\} = Y \) samples belong to a speech utterance of one, two or even more test speakers. The similarity measure should estimate the probability that speaker \( X \) of the training set speaks in \( Y \) speech utterances. Such speaker recognition scenario occurs in forensic evaluation of the evidence using automatic speaker recognition systems. In forensic evaluation speech utterance of a training speaker can be recorded in a separate channel or manually segmented from multi speakers.
speech utterances, and test speech utterances may consist of natural records of persons under investigation.

4.3.1 Features statistics.
In previous section we introduced LPC phase spectrum variation features which for the k-th speech frame consist of \((f_m^k, \delta_m^k)\) pairs where \(f_m^k\) is the frequency position of the m-th local maximum of the group delay and \(\delta_m^k\) a bandwidth of the extremum point. The speech utterances are divided into short time intervals of 1 sec. Duration and distribution of the group delay features of their frames is estimated. Since distance between two neighbor frames is 0.01 sec., we have about \(100(M-1)\) pairs \((f_m^k, \delta_m^k)\) of features in 1 sec. duration utterance. Distribution of \((f_m^k, \delta_m^k) \in (0, \frac{FS}{2}) \times (0, 1)\) is estimated by division of \((0, \frac{FS}{2}) \times (0, 1)\) into \(N \times L\) rectangular boxes and calculating number of pairs \((f_m^k, \delta_m^k)\) that belong to the boxes. Warping parameter \(\lambda = \lambda(FS)\) is adapted to sampling frequency \(FS\) so that division of frequency range \((0, \frac{FS}{2})\) in equal width intervals corresponds roughly to the Bark frequency scale. Possible bandwidth interval \((0, 1)\) is divided into increasing width intervals of total number 10.

4.3.2 Similarity measure of two short speech utterances
Similarity measure between two speech utterances is defined as a mutual information of the two group delay feature distributions. Let \(I = N \times L\) is total number of all possible rectangular boxes \(\{B_i\}_{i=1}^I\) and \(C_X^i = \{c_x^i\}_{i=1}^I\) and \(C_Y^i = \{c_y^i\}_{i=1}^I\) are feature vectors which components are numbers of group delay features belonging to boxes \(B_i\). By definition, all the \(c_x^i\) and \(c_y^i\) correspond to \([x, x+1)\) and \([y, y+1)\) seconds time intervals of \(X\) and \(Y\) speech utterances respectively. Let \(H_X^i\) and \(H_Y^i\) are Shannon’s entropies of the \(C_X^i\) and \(C_Y^i\) counts, i.e.,
\[
H_X^x = - \sum_{i=1}^{l} \frac{c_i^x}{|C_X^x|} \log_2 (\frac{c_i^x}{|C_X^x|}),
\]
(4.19)

\[
H_Y^y = - \sum_{i=1}^{l} \frac{c_i^y}{|C_Y^y|} \log_2 (\frac{c_i^y}{|C_Y^y|}),
\]
(4.20)

\[
|C_X^x| = \sum_{i=1}^{l} c_i^x, |C_Y^y| = \sum_{i=1}^{l} c_i^y.
\]
(4.21)

Let \( C_{X,Y}^x = \{c_i^x + c_i^y\}_{i=1}^l \) denotes conjoint counts of \( C_X^x \) and \( C_Y^y \) and

\[
H_{X,Y}^{x,y} = - \sum_{i=1}^{l} \frac{c_i^{x,y}}{|C_{X,Y}^{x,y}|} \log_2 (\frac{c_i^{x,y}}{|C_{X,Y}^{x,y}|})
\]
(4.22)

is the Shannon's entropy of the \( C_{X,Y}^{x,y} \). It is easy to prove the following statement about a relation between the three entropies.

**Theorem 1.** For any counts \( C_X^x \) and \( C_Y^y \) and their conjoint count \( C_{X,Y}^{x,y} \) the following inequalities hold true:

\[
pH_X^x + qH_Y^y \leq H_{X,Y}^{x,y} \leq pH_X^x + qH_Y^y + H_{p,q},
\]
(4.23)

where

\[
p = \frac{|C_X^x|}{|C_{X,Y}^{x,y}|}, q = \frac{|C_Y^y|}{|C_{X,Y}^{x,y}|} = 1 - p,
\]
(4.24)

and

\[
H_{p,q} = -p\log_2 p - q\log_2 q.
\]
(4.25)

**Proof.** The Gibbs' inequality [17] for any two distributions \( p_i \) and \( q_i \) gives

\[
- \sum_{i=1}^{l} p_i \log_2 p_i \leq - \sum_{i=1}^{l} p_i \log_2 q_i.
\]

Applying this inequality for \( p_i = \frac{c_i^x}{|C_X^x|} \) or \( p_i = \frac{c_i^y}{|C_Y^y|} \) and \( q_i = \frac{c_i^{x,y}}{|C_{X,Y}^{x,y}|} \) we have

\[
pH_X^x + qH_Y^y = - \sum_{i=1}^{l} \frac{c_i^x}{|C_X^x|} \log_2 (\frac{c_i^x}{|C_X^x|}) -
\]

\[
- \sum_{i=1}^{l} \frac{c_i^{x,y}}{|C_{X,Y}^{x,y}|} \log_2 \left( \frac{c_i^{y}}{|C_Y^y|} \right) \leq - \sum_{i=1}^{l} \frac{c_i^{x,y}}{|C_{X,Y}^{x,y}|} \log_2 (\frac{c_i^{x,y}}{|C_{X,Y}^{x,y}|}) = H_{X,Y}^{x,y}
\]

that proves the left hand side inequality of Eq. (4.23).
The right hand side inequality of Eq. (4.23) can be justified by information theory reasoning. $H^x_{X,Y}$ is the average Shannon's information for appearance of a text letter of the text with $C^x_{X,Y}$ letters counts. The information about a letter of the text with conjoint $C^x_{X,Y}$ counts can be obtained using the following procedure. At first the question is asked "is this letter from the text with $C^x_X$ or $C^y_Y$ counts"? Then, depending on the answer to the first question, the second question is asked "which letter is from the text with $C^x_X$ counts?" or "which letter is from the text with $C^y_Y$ counts?" with probability $p$ and $q = 1 - p$ respectively. Answer to the first question contains $H_{p,q} = -p \log_2 p - q \log_2 q$ bits of information and the second one contains $H^x_X$ or $H^y_Y$ bits of information with probability $p$ and $q$ respectively. Since the strategy of provided two questions is not optimal in general, we have the right hand side inequality of Eq. (4.23).

To provide a formal proof of the right hand side inequality of Eq. (4.23) let us consider continuous function:

$$f(x) = -x \log_2(x), x \geq 0.$$ 

It is easy to check that this function is subadditive, that is

$$f(x + y) \leq f(x) + f(y), \forall x, y \geq 0.$$ 

Really, if $y \geq 0$ is fixed then

$$\frac{d}{dx} \left( f(x + y) - f(x) - f(y) \right) = \log_2 \left( \frac{x}{x + y} \right) \leq 0$$

and $f(x + y) = f(x) + f(y)$ at $x = 0$.

Therefore $f(x + y) \leq f(x) + f(y) \forall x, y \geq 0$. Applying this inequality we have:

$$H^x_{X,Y} = - \sum_{t=1}^{l} p c^x_t \log_2 \left( \frac{p c^x_t}{|c^x_X|} \right) + q c^y_t \log_2 \left( \frac{q c^y_t}{|c^y_Y|} \right) \leq$$

$$\leq \sum_{t=1}^{l} p c^x_t \log_2 \left( \frac{p c^x_t}{|c^x_X|} \right) + q c^y_t \log_2 \left( \frac{q c^y_t}{|c^y_Y|} \right)$$

$$= p H^x_X + q H^y_Y + H_{p,q}.$$
Definition 1. Similarity of $p$ of $[x, x + 1]$ time interval (in seconds) of speech utterance of the $X$ speaker to the $[y, y + 1]$ time interval of the $Y$ speaker(s) is the number

$$\rho(X_{[x,x+1]}, Y_{[y,y+1]}) = 1 + \frac{pH_x^X + qH_Y^Y - H_{X,Y}^{x,y}}{H_{p,q}}. \quad (4.26)$$

Theorem 1 gives that the similarity of any two speech utterances $X_{[x,x+1]}$ and $Y_{[y,y+1]}$ is always non-negative and not greater than 1. The next definition gives similarity of $Y_{[y,y+1]}$ short speech utterance to all the $X$ utterances.

Definition 2. Similarity of $Y_{[y,y+1]}$ short speech utterance to the $X$ utterances is the number

$$\rho(X, Y_{[y,y+1]}) = \frac{\sum_{x=0}^{T_x-1} \rho(X_{[x,x+1]}, Y_{[y,y+1]})}{T_x}. \quad (4.27)$$

where $T_x$ is the amount of seconds in $X$ speech utterance. In other words, similarity $\rho(X, Y_{[y,y+1]})$ is the average similarity of $Y_{[y,y+1]}$ utterance to the set of all of one second duration utterances $X_{[x,x+1]}$.

The last definition combines short segments similarities to an integrated similarity of $X$ and $Y$ utterances.

Definition 3. Similarity of $X$ speech utterances to the $Y$ utterances is the number

$$\rho(X, Y) = \text{average value of half biggest } \rho(X, Y_{[y,y+1]}), \quad (4.28)$$

$$y = 0, 1 ... , T_y - 1.$$

The provided similarity measure $\rho(X, Y)$ is asymmetrical (in general $\rho(X, Y) \neq \rho(Y, X)$). This is explained by the asymmetry in $X$ and $Y$ data: $X$ consists of utterances of one speaker and $Y$ may contain utterances of two or even more speakers. If a priori $Y$ contains speech utterances of only one speaker too, the $\rho(X, Y)$ can be modified to symmetrical similarity by skipping "half biggest" words in Definition 3. All provided speech similarity
measures are based on mutual information, are non-negative, and do not exceed 1. If \( X \) and \( Y \) are totally different, i.e. the \( X \) and \( Y \) group delay features points belong to non intersecting sets of boxes \( B_i \), then, with all \( x \) and \( y \), \( H_{X,Y}^{X,Y} = pH_{X}^{X} + qH_{Y}^{Y} + H_{p,q} \) and \( \rho(X,Y) = 0 \). In the opposite case, when the all counts are proportional (\( \forall x, y, i: c_i^x = const \ c_i^y \)) \( H_{X,Y}^{X,Y} = pH_{X}^{X} + qH_{Y}^{Y} = H_{X}^{X} \) and \( \rho(X,Y) = 1 \). Consequently, the similarity measure \( \rho(X,Y) \) has a probabilistic interpretation: \( \rho(X,Y) \) is a probability that \( X \) speaker participates in \( Y \) dialogue.

### 4.4 Experimental Results

#### 4.4.1 Preprocessing of initial data

The following standard steps of initial data preprocessing were used in all our experimentations: Silent or low energy speech intervals were detected and removed from the further analysis, sound data was pre-emphasized with first order filter of the form \( 1 - 0.95z \). speech utterance was segmented into 30 msec. frames with 20 msec. overlapping, frame samples were windowed with Hanning window, first order all-pass filter with warping parameter \( \lambda \approx 0.5 \) [29] was applied to the windowed speech data.

#### 4.4.2 A graphical illustration of group delay features

A speech frame with LPC log power spectrum represented Figure 28 illustrates ideas about group delay features. The first derivative of LPC phase spectrum of the same speech frame is presented in Figure 29. Comparing LPC log power spectrum and LPC phase spectrum variation, one can notice that the last has two additional formants (maximums of the spectrum). The rest five formants of both spectrums have similar positions at frequency axis, however, peaks of the first derivative of LPC phase spectrum are more prominent than that of LPC log power spectrum.
The (4.16) approximation gives a "pole distance" of a chosen formant $f = f_m$ to the unit circle. Figure 30 presents $-\log$ of the distances with marked points that correspond to formats. The coordinates of the marked points define pairs $(f_m, -\log(\delta_m))$ that form features vector of the speech frame.
4.4.3 Experimentation data sets and results

Different speaker recognition techniques were compared using Russian Speech Data voice (RUSBASE) database which is distributed by ELRA (European Language Resources Association) [8] and data from the Netherlands Forensic Institute Speaker Recognition Evaluation (NFISRE). The NFISRE was conducted in 2004 – 2005 in order to compare the methods used by different forensic institutes belonging to the European network of forensic science institutes. NFISRE has two reference recordings containing speech utterances of a known and suspected speaker. Other test recordings contain from 20 sec. to 10 min. speech utterances of two speakers. The NFISRE task was to determine if suspected speaker participates in provided test utterances. Correct training set was constructed by manual segmentation of 2 training recordings leaving only utterances of suspected speaker and recordings that were fully automatically checked. Ideal recognition was obtained by comparing with ground truth released by NFI [9], that is – all impostor and genuine speakers were correctly classified.

RUSBASE is divided into 5 cases with approximately 15 sessions for each case. It contains 44 men and 35 women voices with total size of speech recordings about 500 Mb. First three sessions were used as a training set. Remaining sessions were used for testing.

Table 6: Recognition of RUSBASE speaker, case 1, voice man, using different methods and features

<table>
<thead>
<tr>
<th>Method</th>
<th>Features</th>
<th>EER [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>VQ</td>
<td>MFCC</td>
<td>8.8</td>
</tr>
<tr>
<td>GMM</td>
<td>MFCC</td>
<td>5.8</td>
</tr>
<tr>
<td>GMM</td>
<td>F&amp;A</td>
<td>5.1</td>
</tr>
<tr>
<td>Phonemic</td>
<td>F&amp;A</td>
<td>2.32</td>
</tr>
</tbody>
</table>

RUSBASE recognition based group delay features were compared with Gaussian Mixture Model (GMM) that uses Mel Frequencies Cepstral Coefficients (MFCC), Formants and Antiformants (F&A), pitch value F0. Table 6 [27] gives results of Equal Error Rates (EER) for speaker recognition on
RUSBASE, case 1, men voices, using MFCC, F&A, and F0 features and Vector Quantization (VQ) (see [15]) and GMM recognition methods. The EER ranges from 2.32% to 8.8% (see Table 6). On the group delay and mutual information based speaker recognition algorithm for the same data gives EER = 0.042%.

Table 7 provides full results of speaker recognition of RUSBASE. Here Zero FAR is false acceptance rate (FAR) when false rejection rate (FRR) is 0% and Zero FRR is False rejection rate (FRR) when false acceptance rate (FAR) is 0%.

<table>
<thead>
<tr>
<th>Case</th>
<th>Voice</th>
<th>Zero FAR [%]</th>
<th>EER [%]</th>
<th>Zero FRR [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>man</td>
<td>1.8</td>
<td>0.042</td>
<td>0.12</td>
</tr>
<tr>
<td>1</td>
<td>woman</td>
<td>1.96</td>
<td>0.042</td>
<td>0.07</td>
</tr>
<tr>
<td>2</td>
<td>man</td>
<td>0.8</td>
<td>0.084</td>
<td>0.12</td>
</tr>
<tr>
<td>2</td>
<td>woman</td>
<td>2.17</td>
<td>0.2</td>
<td>1.37</td>
</tr>
<tr>
<td>3</td>
<td>man</td>
<td>3.19</td>
<td>0.058</td>
<td>0.09</td>
</tr>
<tr>
<td>3</td>
<td>woman</td>
<td>1.96</td>
<td>0.033</td>
<td>0.06</td>
</tr>
<tr>
<td>4</td>
<td>man</td>
<td>0.6</td>
<td>0.01</td>
<td>0.02</td>
</tr>
<tr>
<td>4</td>
<td>woman</td>
<td>4.6</td>
<td>0.112</td>
<td>0.15</td>
</tr>
<tr>
<td>5</td>
<td>man</td>
<td>2.79</td>
<td>0.199</td>
<td>0.59</td>
</tr>
<tr>
<td>5</td>
<td>woman</td>
<td>0.44</td>
<td>0.007</td>
<td>0.01</td>
</tr>
</tbody>
</table>

The new speaker recognition technique showed a reduction of equal error rate up to twenty times in comparison to traditional methods that use features derived exclusively from the amplitude of the power spectrum.

4.5 Summary and Conclusions of the Chapter

It is shown that phase of transfer function defined by linear prediction model can be used for derivation of features of utterances. The features represent extremes of the group delay of the LP model. Similarity measure between two speech utterances was defined as mutual information of the two group delay feature distributions. The performance of group delay features and their similarity metric was tested on two speaker datasets that contain text-dependent and text-independent utterances. The new speaker recognition technique showed up a reduction of equal error rate up to twenty times in
comparison to traditional methods that use features derived exclusively from the amplitude of the power spectrum.

5 Fusion

5.1 Introduction
Fingerprint recognition and speaker recognition alone are widely used to solve tasks such as time-attendance control, data encryption, system logon and others, but when top security is required in applications such as bank account protection, border control or law enforcement, one modality is not enough. Manual workers or elderly people have worn fingerprints with lots of scars and imperfections so using only fingerprints may lead to high false rejection rate. Similar problems can happen to a person’s voice. Each biometric has its own vulnerabilities. Security system based on fingerprints can be attacked using artificial (gummy) fingers. Multibiometrics can help in making biometric system more flexible and secure. This chapter focuses on multibiometrics using speaker recognition and fingerprint recognition. The performance of three biometric systems (biometric system based upon single fingerprint, two fingerprints and multibiometric system based on fingerprints and voice) is compared.

5.2 Testing data
Since all above mentioned databases contained only voice samples or only fingerprints the need for a new database appeared. No publicly available multimodal fingerprint and voice database was found, so new database was prepared to evaluate finger and voice fusion. The database consists from two parts: voice and fingerprint.
5.2.1 Voice database
Voice database was recorded in natural office conditions using low cost headset ACME HM – 03. There were two recording sessions with an interval no less than a week to imitate natural usage scenario.

Voice samples were taken from 23 persons. Each person was asked to say two types of phrases – fixed (F) and not fixed (NF). Fixed type of phrase consisted of numbers from 1 to 10 (in Lithuanian language). This type of phrase was the same for each person. The duration of the phrase is about 10 seconds.

Not fixed type of phrase was different for each person and consisted of several words: the person was asked to say name, surname and living address (street, number of the house and room number). The duration of the phrase is also about 10 seconds.

5.2.2 Fingerprints database
Fingerprints were taken from the same 23 persons. Lumidigm Venus V302 fingerprint scanner was used to capture the fingerprints. There were 10 fingerprint scanning sessions. Interval between sessions was not as long as interval between voice recording sessions because fingerprints are not as variable as voice.

5.3 Fusion
In this chapter following fusion strategies are compared: fingerprint + fingerprint and fingerprint + voice.

5.3.1 Fingerprint + fingerprint fusion
Fingerprints were enrolled using extraction algorithm COMM mentioned in the second chapter [23] and matched using algorithm described in second chapter.

Since there were 10 scanning sessions there are 10 instances of each fingerprint that belong to the same person (genuine). Similarity scores can be
combined in many ways. For example similarity scores from index fingers can be combined, or from thumbs.

To investigate the possibilities of fingerprint fusion, correlation between fingerprints was calculated in the following way: a fingerprint position was selected, for example, right index finger. Since we have 23 persons scanned 10 times, we have 230 instances of right index finger. 10 instances are genuine and 220 instances are impostors. Only genuine pairs were taken into consideration because in most cases similarity between impostors is zero. Similarities between genuine pairs were calculated giving us a column of similarities. Then another fingerprint was selected, for example left index finger. Similarities between genuine pairs were calculated in the same order as the similarities of genuine pairs of right index giving us another column of similarities. Correlation coefficient between these two columns shows how much left index finger correlates with right index finger. The above procedure was repeated for all possible fingerprint pairs (left index + right index, left index + right thumb, left thumb + right index and so on) giving us the following table (Table 8) where fingers are numbered in a following way: 1, 2, 3, 4 and 5 are right thumb, right index, right middle, right ring, and right small; 6, 7, 8, 9, 10 are left thumb, left index, left middle, left ring, and left small.
Table 8: Correlations between fingerprints with different positions.

<table>
<thead>
<tr>
<th>Finger</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>.21 ± .04</td>
<td>.21 ± .04</td>
<td>.3 ± .04</td>
<td>.19 ± .04</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>.33 ± .04</td>
<td>.34 ± .03</td>
<td>.33 ± .04</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>.3 ± .04</td>
<td>.33 ± .04</td>
<td>.44 ± .04</td>
<td>.37 ± .04</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>.3 ± .04</td>
<td>.33 ± .04</td>
<td>.37 ± .04</td>
<td>.37 ± .037</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>.33 ± .04</td>
<td>.37 ± .04</td>
<td>.37 ± 037</td>
<td>.1</td>
</tr>
<tr>
<td>6</td>
<td>.24 ± .04</td>
<td>.11 ± .04</td>
<td>.16 ± .04</td>
<td>.19 ± .05</td>
<td>.09 ± .05</td>
</tr>
<tr>
<td>7</td>
<td>.10 ± .04</td>
<td>.10 ± .05</td>
<td>.07 ± .05</td>
<td>.09 ± .04</td>
<td>.06 ± .05</td>
</tr>
<tr>
<td>8</td>
<td>.10 ± .04</td>
<td>.13 ± .04</td>
<td>.14 ± .05</td>
<td>.26 ± .04</td>
<td>.20 ± .05</td>
</tr>
<tr>
<td>9</td>
<td>.14 ± .04</td>
<td>.08 ± .04</td>
<td>.15 ± .04</td>
<td>.29 ± .04</td>
<td>.22 ± .04</td>
</tr>
<tr>
<td>10</td>
<td>.27 ± .04</td>
<td>.20 ± .04</td>
<td>.12 ± .04</td>
<td>.12 ± .04</td>
<td>.26 ± .04</td>
</tr>
</tbody>
</table>

Table 8 continued.

<table>
<thead>
<tr>
<th>Finger</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>.24 ± .04</td>
<td>.10 ± .04</td>
<td>.05 ± .04</td>
<td>.14 ± .04</td>
<td>.27 ± .04</td>
</tr>
<tr>
<td>2</td>
<td>.11 ± .04</td>
<td>.10 ± .05</td>
<td>.13 ± .04</td>
<td>.07 ± .04</td>
<td>.20 ± .04</td>
</tr>
<tr>
<td>3</td>
<td>.16 ± .04</td>
<td>.07 ± .05</td>
<td>.14 ± .05</td>
<td>.15 ± .04</td>
<td>.12 ± .04</td>
</tr>
<tr>
<td>4</td>
<td>.19 ± .05</td>
<td>.09 ± .04</td>
<td>.26 ± .04</td>
<td>.29 ± .04</td>
<td>.12 ± .04</td>
</tr>
<tr>
<td>5</td>
<td>.09 ± .05</td>
<td>.06 ± .04</td>
<td>.20 ± .05</td>
<td>.22 ± .04</td>
<td>.26 ± .04</td>
</tr>
<tr>
<td>6</td>
<td>.17 ± .04</td>
<td>.17 ± .04</td>
<td>.20 ± .04</td>
<td>.20 ± .04</td>
<td>.30 ± .04</td>
</tr>
<tr>
<td>7</td>
<td>.17 ± .04</td>
<td>.17 ± .04</td>
<td>.25 ± .05</td>
<td>.12 ± .05</td>
<td>.21 ± .04</td>
</tr>
<tr>
<td>8</td>
<td>.20 ± .04</td>
<td>.25 ± .05</td>
<td>.1</td>
<td>.30 ± .03</td>
<td>.21 ± .04</td>
</tr>
<tr>
<td>9</td>
<td>.20 ± .04</td>
<td>.12 ± .05</td>
<td>.30 ± .04</td>
<td>.1</td>
<td>.32 ± .04</td>
</tr>
<tr>
<td>10</td>
<td>.30 ± .04</td>
<td>.21 ± .04</td>
<td>.21 ± .04</td>
<td>.37 ± .04</td>
<td>.1</td>
</tr>
</tbody>
</table>

It is easy to notice that the smallest correlation is between fingers with positions 1 (right thumb) and 8 (left middle) (0.050 ± 0.041). The largest correlation is between fingers with positions 3 (right middle) and 4 (right ring) (0.439 ± 0.035).

ROC curves were calculated for each fingerprint. FRR@FAR = 0% (Zero FAR) and equal error rate (EER) are presented in Table 9.
Table 9: FRR@FAR = 0% and EER of fingerprint recognition algorithm (fingers 1 – 10).

<table>
<thead>
<tr>
<th>Finger position</th>
<th>Zero FAR[%]</th>
<th>EER[%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.67</td>
<td>0.64</td>
</tr>
<tr>
<td>2</td>
<td>0.56</td>
<td>0.31</td>
</tr>
<tr>
<td>3</td>
<td>4.17</td>
<td>1.80</td>
</tr>
<tr>
<td>4</td>
<td>6.76</td>
<td>2.51</td>
</tr>
<tr>
<td>5</td>
<td>5</td>
<td>1.72</td>
</tr>
<tr>
<td>6</td>
<td>2.78</td>
<td>1.94</td>
</tr>
<tr>
<td>7</td>
<td>1.39</td>
<td>0.86</td>
</tr>
<tr>
<td>8</td>
<td>4.35</td>
<td>1.63</td>
</tr>
<tr>
<td>9</td>
<td>7.96</td>
<td>3.15</td>
</tr>
<tr>
<td>10</td>
<td>5.93</td>
<td>2.50</td>
</tr>
</tbody>
</table>

Since correlations between fingerprints are low, fusion could give good results. It is natural to fuse symmetric fingerprints (left index with right index, left thumb with right thumb), so only symmetric fingerprints were fused by simple summation rule. ROCs of fused fingerprints were calculated and the results of the fusion summarized in Table 10:

Table 10: FRR@FAR = 0% (Zero FAR) and EER values of fused fingerprints ROC.

<table>
<thead>
<tr>
<th>Fingers</th>
<th>Zero FAR[%]</th>
<th>EER[%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1+6</td>
<td>0.09</td>
<td>0.08</td>
</tr>
<tr>
<td>2+7</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>3+8</td>
<td>0.46</td>
<td>0.17</td>
</tr>
<tr>
<td>4+9</td>
<td>0.83</td>
<td>0.18</td>
</tr>
<tr>
<td>5+10</td>
<td>0.28</td>
<td>0.11</td>
</tr>
</tbody>
</table>

It is easy to notice from Table 9 and Table 10 that matching reliability becomes more than two times better when two fingerprints are used instead of one. Fusion of voice and fingerprints is described in next section.

5.3.2 Fingerprint + voice fusion

ROCs on voice database were calculated. Different usage scenarios were analyzed: Not fixed vs. not fixed (NF vs. NF); fixed vs. fixed (F vs. F); NF vs. F and F vs.NF. FRR@FAR = 0% and EER values of ROCs are presented in Table 11.
Table 11: FRR@FAR = 0% (Zero FAR) and EER values of speaker recognition algorithm.

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Zero FAR[%]</th>
<th>EER[%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>NF vs. NF</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>F vs. F</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>NF vs. F</td>
<td>78.26</td>
<td>10</td>
</tr>
<tr>
<td>F vs. NF</td>
<td>47.82</td>
<td>9.75</td>
</tr>
</tbody>
</table>

It is obvious that when same type voice phrases are used, the recognition is ideal (algorithm makes no errors), but when different type of voice phrases are used (more natural scenario), the recognition performance is not as good as fingerprint recognition (what is widely known, since voice is more variable than fingerprint).

To investigate fingerprint and voice fusion, correlations between fingerprints and voice of the same person were calculated in the following way: fixed type of voice sample was matched against not fixed type of voice sample (since F vs. NF scenario performance is better than NF vs. F) giving us a voice similarity score. Fingerprints of the same person were matched against each other and lowest similarity score was taken giving us finger similarity score. Lowest similarity score was taken to analyze the most difficult case.

Correlation between 23 voice and 23 fingerprint similarities was calculated giving value \(-0.110 \pm 0.251\), so good fusion might be expected.

ROCs for three scenarios were calculated: single finger, two finger fusion (symmetric fingers were used like in Table 10) and finger and voice fusion. Similarity scores of fingerprint and voice algorithms were normalized to have the same mean and standard deviation. After that they were simply added. The results are summarized in Table 12 (FRR@FAR = 0%) and Table 13 (EER).
Table 12: Comparison of three scenarios FRR @ FAR = 0% [%].

<table>
<thead>
<tr>
<th></th>
<th>Single Finger</th>
<th>Two Fingers</th>
<th>Finger and Voice</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.67</td>
<td>1+6</td>
<td>0.09</td>
</tr>
<tr>
<td>2</td>
<td>0.56</td>
<td>2+7</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>4.17</td>
<td>3+8</td>
<td>0.46</td>
</tr>
<tr>
<td>4</td>
<td>6.76</td>
<td>4+9</td>
<td>0.83</td>
</tr>
<tr>
<td>5</td>
<td>5</td>
<td>5+10</td>
<td>0.28</td>
</tr>
<tr>
<td>6</td>
<td>2.78</td>
<td>6+1</td>
<td>0.09</td>
</tr>
<tr>
<td>7</td>
<td>1.39</td>
<td>7+2</td>
<td>0</td>
</tr>
<tr>
<td>8</td>
<td>4.35</td>
<td>8+3</td>
<td>0.46</td>
</tr>
<tr>
<td>9</td>
<td>7.96</td>
<td>9+4</td>
<td>0.83</td>
</tr>
<tr>
<td>10</td>
<td>5.93</td>
<td>10+5</td>
<td>0.28</td>
</tr>
</tbody>
</table>

It can be seen from Table 12 that in all cases finger and voice fusion performers better than single fingerprint no matter what characteristic (Zero FAR or EER) is considered.

In cases where correlation between two fingers is high, voice and fingerprint fusion performs even better than two fingerprints fusion (see Table 12 row 1 (single fingerprint – 0.64%, two fingerprints – 0.09%, voice and fingerprint – 0%), row 3 (single fingerprint – 4.17%, two fingerprints – 0.46%, voice and fingerprint – 0.22%), and Table 13 rows 1 and 3).

Table 13: Comparison of three scenarios EER [%].

<table>
<thead>
<tr>
<th></th>
<th>Single Finger</th>
<th>Two Fingers</th>
<th>Finger and Voice</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.64</td>
<td>1+6</td>
<td>0.08</td>
</tr>
<tr>
<td>2</td>
<td>0.31</td>
<td>2+7</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>1.80</td>
<td>3+8</td>
<td>0.17</td>
</tr>
<tr>
<td>4</td>
<td>2.51</td>
<td>4+9</td>
<td>0.18</td>
</tr>
<tr>
<td>5</td>
<td>1.72</td>
<td>5+10</td>
<td>0.11</td>
</tr>
<tr>
<td>6</td>
<td>1.94</td>
<td>6+1</td>
<td>0.08</td>
</tr>
<tr>
<td>7</td>
<td>0.86</td>
<td>7+2</td>
<td>0</td>
</tr>
<tr>
<td>8</td>
<td>1.63</td>
<td>8+3</td>
<td>0.17</td>
</tr>
<tr>
<td>9</td>
<td>3.15</td>
<td>9+4</td>
<td>0.18</td>
</tr>
<tr>
<td>10</td>
<td>2.50</td>
<td>10+5</td>
<td>0.11</td>
</tr>
</tbody>
</table>
5.4 Summary and Conclusions of the Chapter

Multibiometrics using fingerprints and voice was presented in this chapter. Experiments show major increase in identification performance. Multibiometric systems have many advantages over systems limited to only one modality. They are more flexible and secure.

6 Conclusions

Fingerprint image synthesis method and two biometric algorithms (person identification by fingerprints and speaker identification by voice) were described in detail.

The speed of an earlier known synthesis algorithm has increased more than three times. A new practical application of synthetic fingerprints to estimate the quality of a fingerprint image by comparing it to an ideal noise free synthetic fingerprint was found.

Problems in fingerprint matching are analyzed, and necessity of registration (evaluation of rotation and translation) is discussed.

New Fingerprint matching algorithm is designed to match deformed fingerprints. It consists of simple and intuitive steps. The proposed implementation of the steps is straightforward and flexible, does not use registration, and therefore is capable of matching deformed fingerprints. The advantage of proposed fingerprint matching algorithm is validated on a set of popular publically available fingerprint databases. One-tailed t-test showed improvement in comparing with NIST matcher with $p < 0.0005$.

Speaker recognition algorithm uses phase of transfer function defined by linear prediction model for derivation of features of utterances. The features represent extremes of the group delay of the LP model. Similarity measure between two speech utterances was defined as a mutual information of the two group delay feature distributions.
The proposed voice recognition algorithm showed up to ten times better performance in comparison with commonly accepted on Gaussian Mixture Model based voice recognition algorithm.

Multibiometrics using fingerprints and voice was also presented. Experiments showed significant decrease in EER and FRR@FAR = 0% when two fingerprints or fingerprint and voice are used.

Voice and fingerprint fusion performs almost as well as two fingerprints fusion.

This study is the first to demonstrate that similarities between voice samples and similarities between fingerprints do not have any correlation what makes them ideal for multibiometric.

**6.1 Future Directions**

Fingerprint synthesis method (chapter 2) can be used to create a fingerprint with pre-defined properties and features. It would be interesting to investigate the possibilities of synthesis to reconstruct low quality fingerprints with scars, dirt and other imperfections.

During developing and testing of the fingerprint matching algorithm (chapter3), minutiae features were limited to position and direction information. Addition of other features (minutiae type, quality, texture information) could further improve matcher performance.

It was shown that fingerprint fusion and voice fusion performs better than fingerprints alone (chapter 5), and in some cases fingerprint and voice fusion performs even better than fingerprint fusion. Such cases occur when correlation between fingerprints is high. It would be useful to investigate such occurrences and introduce additional normalization in fusion rule to account fingerprint correlation.
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Acronyms

AFIS  Automatic Fingerprint Identification System
FVC  Fingerprint Verification Competition
NIST  National Institute of Standards and Technology
MINEX  Minutiae Interoperability Exchange Test
ROC  Receiver Operating Characteristic
DET  Detection Error Tradeoff
SFINGE  Synthetic Fingerprint Generation
EDM  Euclidean Distance Map
WSQ  Wavelet Scalar Quantization
DPI  Dots per Inch
FRR  False Rejection Rate
FAR  False Acceptance Rate
EER  Equal Error Rate
NFIS2  NIST Fingerprint Image Software Version 2
GMM  Gaussian Mixture Model
LP  Linear Prediction
LPC  Linear Prediction Coefficient
NFISRE  Netherlands Forensic Institute Speaker Recognition Evaluation
RUSBASE  Russian Speech Data voice