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#### PAPER

## Phonon-assisted leakage current of InGaN light emitting diode

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#### Abstract

We report on the leakage current mechanism in a blue GaN-based light-emitting diode (LED). The device structure was grown by the MOCVD technique on a sapphire substrate. The LED was characterized through various measurements including current-voltage, electroluminescence, and secondary ion mass spectroscopy (SIMS). Capacitance-voltage measurements were employed to calculate the depletion layer thickness at different bias voltages and to analyze the doping profile in the active layer. The reverse temperature-dependent current-voltage measurements were carried out to study the leakage mechanism. The leakage current was explained by phonon-assisted tunneling of charge carriers through deep trap states. The trap energy and density of states were extracted from the application of the introduced model. Cathodoluminescence measurements were performed to evaluate the density of dislocations, which were then compared to x-ray diffraction measurements. The determined value was close to the density of states obtained from the tunneling model.

#### 1. Introduction

GaN-based materials are III/V group direct bandgap semiconductors used in optoelectronic devices, such as light-emitting diodes(LEDs). Studies on the leakage current mechanism of these devices are of particular importance due to their immense potential to further increase reliability and energy efficiency, especially when reducing the size of the devices. GaN technology still faces a problem: the absence of cost-effective bulk substrates for homoepitaxy. Most of the GaN layer growth is conducted on thermal coefficient and latticemismatched substrates such as sapphire, silicon, or SiC[[1](#page-6-0)]. This leads to the presence of imperfections inside the crystal including extended defects such as various types of dislocations. The extended defects, particularly threading dislocations, can propagate throughout the entire structure of the device, creating spatially closed defect states[[2](#page-6-0)]. These defects are responsible for the leakage current in the space charge region of the p–n junction [[3](#page-6-0)]. Studies show that the carrier transport mechanism is dominated by tunneling through the deep defect states within the band gap. Reverse [[4](#page-6-0)–[7](#page-6-0)] or low current direct [[8,](#page-6-0) [9](#page-6-0)] temperature-dependent currentvoltage measurements are usually performed to analyze the leakage mechanism.

Recently, various attempts have been made to model reverse leakage currents in GaN-based structures, employing mechanisms such as the Pool-Frenkel effect and trap-assisted tunneling  $[10, 11]$  $[10, 11]$  $[10, 11]$  $[10, 11]$  $[10, 11]$ . However, these models exhibit limitations in the two key areas: matching experimental data across a wide temperature range, and establishing a strong relationship between the extracted parameters and the crystalline quality of GaN-based materials.

In contrast, the phonon-assisted tunneling model, introduced by P. Pipinyset al [[12](#page-6-0)], has demonstrated good agreement with the reverse current-voltage characteristics of the nGaN Schottky diode structure across a wide temperature range. Efforts have also been made to apply this model for the explanation leakage currents in high mobility transistors(HEMTs) [[13](#page-6-0)]. In our current study, we investigate the applicability of this model to a more complex LED device structure. We conduct a detailed current-voltage, electroluminescence characterization of the as-grown LED device. The second ion mass spectroscopy (SIMS) and

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<span id="page-1-0"></span>

determined by SIMS. Dashed curves indicate the boundaries of corresponding layers (b). Concentration  $N_{CV}$  extracted from CV profile measured at room temperature (solid curve). The dashed curve shows the Si donor concentration  $N_D$  injected during MOCVD growth (c). Forward and reverse current-voltage curves(d). Electroluminescence at different injection currents(e). Efficiency as a function of current(f).

capacitance-voltage (CV) measurements we performed to analyze the doping concentration, focusing on the active layer of LED. We have demonstrated that the density of defect states extracted from reverse currentvoltage characteristics at different temperatures can be directly related to the density of threading dislocations. The threading dislocation density was measured by means of cathodoluminescence and further validated through XRD analysis in the current paper.

## 2. Experimental

The metal face III-nitride epitaxial layers of the LED were grown on a c-plane sapphire substrate using an AIXTRON (3x2) metal-organic chemical vapor deposition (MOCVD) reactor. The mesa structures were fabricated through photolithography using laser writing equipment, followed by inductively coupled plasma reactive ion etching (ICP-RIE) from Oxford Instruments. A gas mixture of Ar/Cl<sub>2</sub> was used for dry etching at a rate of 5 nm/s. The ICP-RIE etched profile exhibits a steepness of around 75°. To remove native oxide and to minimize current leakage caused by surface imperfections after RIE, we performed an HF acid treatment on the structures. For the contacts, we utilized e-beam-evaporated Ni/Au and Ti/Au metals for Mg-doped p-type and Si-doped n-type GaN, respectively. The mesas of devices had dimensions of 270  $\times$  270  $\mu$ m<sup>2</sup>. The structure of the LED cross-section is depicted in figure 1(a) and consists of an n-type GaN layer, an eight-period GaN/InGaN superlattice (SL), a five-period GaN/InGaN multiple quantum wells(MQW), an n-type GaN cap layer, an AlGaN electron-blocking layer, and is finished with a p-type GaN layer. The p-type Mg dopant, as well as the distribution profile of III group elements determined by secondary ion mass spectroscopy (SIMS) is shown in figure 1(b). The distribution of donor concentration  $N_D$  in the vicinity of the MQW active layer evaluated from the flows of the MOCVD process is illustrated in figure  $1(c)$  for comparison with the corresponding capacitancevoltage (CV) measurement results. The CV characterization was achieved using Keithley 4200-CVU module, integrated within the Keithley 4200-SCS Semiconductor Characterization System. Cathodoluminescence images were taken at room temperature with an acceleration voltage set to 4 kV. Depending on the magnification, the e-beam was scanned in steps of 14-to-46 nm with a dwell time set to 1 ms. Automatic defect/ dislocation identification was performed using a custom Python code and the Laplacian of Gaussian Blob Detection algorithm from scikit-image library  $[14]$  $[14]$  $[14]$ . Additionally, the x-ray diffraction method (XRD) with a Cu Kα radiation source was used to evaluate the screw-type dislocation density and to confirm the cathodoluminescence measurement results.

#### <span id="page-2-0"></span>3. Results and discussion

#### 3.1. Characterization of LED device

The LED for studying leakage mechanisms was fabricated with an additional embedded Si-doped GaN layer on top of the multiple quantum well (MQW) structure. This layer affects the band structure of the device by shifting the MQW region towards the n-type side of the junction, resulting in a more abrupt p–n junction. The electric field distribution in the space charge region of such an LED structure is similar to that of a GaN p–n junction without the MQW.

Figure [1](#page-1-0)(d) presents the forward and reverse current-voltage characteristics of the LED measured at room temperature, plotted in semi-log scale. The device exhibits good rectifying behaviour, with a reverse leakage current as low as  $10^{-7}$  A at 10 V. The forward current-voltage curve is linear in semi-log scale up to 3 V. The dependence in this region can be described by Shockley's diode equation:  $I = I_0 \exp(qV/(n_i k_B T))$ , where  $I_0$  is the pre-exponential factor, q is the elementary charge, V is the bias voltage,  $n_i$  is the ideality factor,  $k_B$  is the Boltzmann constant, and T is the absolute temperature. According to this equation, it was found that  $n_i = 4.6$ . An ideality factor larger than 2 is a criterion for dominating tunneling in the charge transport mechanism.

Figure [1](#page-1-0)(e) displays the electroluminescence measurement spectra at different injection currents. The peak maximum of the emitted light is at a wavelength of 434 nm, and it remains stable over the entire measured current range. This stability can be attributed to the design of the LED, which minimizes the impact of changes in the built-in potential on the energy levels of the states within the multiple quantum wells(MQWs)when forward current is applied. The ratio of light emission power to electrical power, or LED efficiency, versus injection current is presented in figure [1](#page-1-0)(f). The LED efficiency increases up to 30 mA, after which the efficiency droop effect is observed. This phenomenon is typical for LED devices [[15](#page-6-0)].

#### 3.2. CV measurement analysis

The CV measurements were performed at 1 MHz using an altering current signal level of 15 mV under ambient conditions at room temperature. The dopant concentration can be calculated by the following equation:

$$
N_{CV} = \frac{2}{q\varepsilon\varepsilon_0 A^2 d(1/C^2)/dV}
$$
 (1)

where  $\varepsilon$  and  $\varepsilon_0$  are relative and absolute dielectric constants, respectively. A is the area of the device, C is the measured capacitance at corresponding bias voltage V. The depletion width W is related to capacitance as  $W = \varepsilon \varepsilon_0 A/C$ . By employing the equations mentioned above, the dopant concentration profiles can be determined. Figure [1](#page-1-0)(c) displays the solid curve, which represents the CV profile plot of the LED. Periodic damping peaks are observed in the MQWs region, and the distance between these peaks is approximately 9 nm, corresponding to the period of the MOWs  $[4, 16]$  $[4, 16]$  $[4, 16]$  $[4, 16]$  $[4, 16]$ . Additionally, some periodic steps can be identified in the adjacent InGaN SL region, which is close to the periodicity 3 nm of the SL structure.

The acceptor level of Mg is deep within a band gap, it can make complexes with hydrogen during MOCVD growth and suffers from self-compensation effect [[17](#page-6-0), [18](#page-6-0)]. A high number of Mg atoms are needed to reach sufficient conductivity. However, when a p–n junction is formed especially in a reverse bias regime the band bending occurs. This effect results in a change in the ionization state of Mg and leads to a high ionized acceptor concentration in the depletion region [[19](#page-6-0)]. Therefore, the p–n junction is highly asymmetric in GaN-based material with the depletion region penetrating into the n-side of the junction. This situation is shown in figure [2](#page-3-0) where modeled n-side and total depletion width curves are close to each other.

The total depletion width can be evaluated by the following equation:

$$
W = \sqrt{\frac{2\varepsilon\varepsilon_0}{q}(V_0 - V)\left(\frac{1}{N_A} + \frac{1}{N_D}\right)}
$$
(2)

where built-in voltage ( $V_0$ ) is equal to 3.3 V, and V is the applied reverse bias voltage. At zero bias, the depletion width is approximately 30 nm. The curves shown in figure [2](#page-3-0) were modeled with donor and acceptor concentrations at values  $N_D = 2 \cdot 10^{18}$  cm<sup>-3</sup> and  $N_A = 4 \cdot 10^{19}$  cm<sup>-3</sup>, respectively. The  $N_D$  value corresponds to the average donor concentration obtained from CV dopant profile above a depletion width of 30 nm (figure [1](#page-1-0)(c)). Additionally, the  $N_A$  value is attributed to the average Mg dopant concentration in the p-type electron blocking layer determined from SIMS analysis(figure [1](#page-1-0)(e)). The curve extracted from CV measurements(figure [2](#page-3-0)) demonstrates good agreement with the calculated total depletion width values above the reverse voltage of 5 V. However, in the low voltage range, the CV curve falls below the modeled values. To achieve a better fit with the CV curve in the low voltage range, the dopant concentration  $N_D$  should be increased to around 3·10<sup>18</sup> cm<sup>-3</sup>, considering that the depletion width (equation (2)) is inversely proportional to the dopant concentration. The increased dopant concentration in the low voltage range coincides with the CV profile rather than the Si dopant profile (see figure [1](#page-1-0)). It should be emphasized, that the indium concentration is

<span id="page-3-0"></span>

higher in the InGaN solid solution of the MQW compared to the SL of the produced LED. The indium-induced defects can contribute to the higher  $N_{CV}$  concentration observed in the MQW region.

#### 3.3. Interpretation of reverse leakage current

Numerous studies on the reverse leakage current of LEDs demonstrate that a high amount of energy is required to excite trapped charge carriers from states within the band gap. This conduction mechanism can be explained by multi-step tunneling through these deep states. In such a case, the leakage current Iis directly proportional to the number of states  $N_s$  and the tunneling rate P:

$$
I = qA N_s P \tag{3}
$$

For phonon-assisted charge carrier tunneling, the rate depends on temperature T and electric field E. If the tunneling process occurs through a triangular barrier of depth  $\varepsilon_T$ , the tunneling rate can be described as [[12](#page-6-0)]:

$$
P = \frac{eE}{(8m^* \varepsilon_T)^{1/2}} [(1 + \gamma^2)^{1/2} - \gamma]^{1/2} [1 + \gamma^2]^{-1/4}
$$
  
 
$$
\times \exp \left\{ -\frac{4}{3} \frac{(2m^*)^{1/2}}{eE\hbar} \varepsilon_T^{3/2} [(1 + \gamma^2)^{1/2} - \gamma]^2 \right\}
$$
  
 
$$
\times \left[ (1 + \gamma^2)^{1/2} + \frac{1}{2} \gamma \right] \right\}
$$
 (4)

where

$$
\gamma = \frac{(2m^*)^{1/2}\Gamma^2}{8e\hbar E \varepsilon_T^{1/2}}
$$
\n(5)

The  $\Gamma = 8a(\hbar\omega)^2(2n+1)$  represents the width of the center absorption band with a phonon distribution function  $n = [exp(\hbar \omega)/(k_B T) - 1]^{-1}$ . The parameter *a* is a charge carrier-phonon interaction constant, and  $\hbar\omega$  is phonon energy.

The average electric field in the depletion region of the LED can be evaluated using  $E = (V_0 - V)/W$ . By substituting equation ([2](#page-2-0)) into the electric field expression, one can obtain that the average internal electric field is proportional to the square root of the total electrostatic potential, i.e.,  $E \sim \sqrt{(V_0 - V)}$ . This relationship, along with the proportionality constant that includes donor and acceptor concentration values given in the inset of figure 2, was incorporated into the tunneling model to fit the experimental measurements. Figure [3](#page-4-0) displays the current-voltage characteristics along with the modeling results at different temperatures. Two main parameters, trap energy, and density of states were varied to obtain the best fitting results. We found that trap energy can be as high as 0.89  $\pm$  0.01 eV, while density of states is equal to 4.6·10<sup>8</sup>  $\pm$  1.6·10<sup>8</sup> cm<sup>-2</sup>. The other parameters remained the same as in [[12](#page-6-0)], except for the effective mass. Unlike the Schottky diode analyzed in [[12](#page-6-0)], the LEDs contain GaN/AlGaN heterostructures. Therefore, the effective mass of electrons can be as high as  $0.4m_e$  [[20,](#page-6-0) [21](#page-6-0)].

<span id="page-4-0"></span>





4 keV electrons in the nGaN layer of the LED and measured at a wavelength of 363 nm; the inset shows the spatially averaged cathodoluminescence spectrum.

Figure 3 demonstrates that the phonon-assisted tunneling model does not fit the experimental data well below 5 V. When using the depletion width values extracted from CV measurements and substituting them into the model, there is an even higher deviation in the low voltage range. For the triangular tunneling barrier depicted in figure 4(a), the tunneling length L can be determined using the relationship  $qEL = \varepsilon_T C_\gamma^{2/3}$ , where  $C^{2/3}_\gamma$  represents the term with variables  $\gamma$  inside the exponent of equation ([4](#page-3-0)). The calculated tunneling length



values, obtained from this relationship, vary from 5.3 nm to 4.5 nm in the range of 5-10 V at room temperature. These values are reasonable for the tunneling process. However, the high tunneling length at a lower bias voltage can lead to a deviation from the presented model.

Figure  $4(b)$  $4(b)$  shows the cathodoluminescence (CL) intensity distribution map with a peak wavelength of 363 nm. This photon emission wavelength corresponds to the direct band gap charge carrier recombination process in GaN. The CL mapping was obtained in the area of the RIE-etched LED, reaching the nGaN layer close to the exact device under investigation. Dislocation defects in GaN are active non-radiative recombination centers, resulting in the reduced intensity of CL. To quantify the dislocation density, we performed a numerical analysis of the CL image, identifying the number of dark areas. Consequently, the average number of dislocations was found to be 4.3·10 $^8\pm\,$  2.7·10 $^8$  cm<sup>-2</sup>, a value very close to the density of states determined by the phonon-assisted tunneling model.

High-resolution XRD analysis of the LED structure is shown in figure 5. The XRD rocking curve measurement of reflection from the GaN(0002) lattice plane revealed a full width at half maximum (FWHM) equal to 332 arcseconds. According to the model proposed by Dunn and Koch [[22](#page-6-0)], the density of screw-type threading dislocations can be calculated using the equation  $\varrho=\beta^2/(4.36b^2)$ , where  $\beta$  is the peak broadening and b is the magnitude of the Burgers vector. This model gives a screw-type threading dislocation density value of  $\rho = 2.2 \cdot 10^8$  cm<sup>-2</sup>. This value is in the same order of magnitude, although about half, of the threading dislocation density determined by cathodoluminescence. The observed mismatch may be due to measurements of slightly different locations on the same wafer. Additionally, some other technical factors such as probing depth, that come from the origin of these two methods can lead to the difference observed [[23](#page-6-0)].

## 4. Conclusions

In summary, we analyzed the CV measurements and IV characteristics of GaN-based LED with a peak wavelength at 434 nm. We employed a phonon-assisted tunneling model to fit the reverse IV experimental data in the temperature range 296-523 K. The model showed good fitting results at a higher bias voltage above 5V. The tunneling occurs from the deep-state traps of energy 0.89 eV, which are responsible for the internal leakage current. Our findings revealed, that the density of states (4.6·10<sup>8</sup> cm<sup>-2</sup>) shows good agreement with the number of dislocations (4.3·10<sup>8</sup> cm<sup>-2</sup> from CL measurements and 2.2·10<sup>8</sup> cm<sup>-2</sup> from XRD analysis). The formation of dislocations during the epitaxy of LED leads to a higher density of deep traps.

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#### Data availability statement

All data that support the findings of this study are included within the article (and any supplementary files).

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